

Topic :- Dual nature of radiation and matter

- 2 (b)
With the increase in intensity of light photoelectric current increases, but kinetic energy of ejected electron, stopping potential and work function remains unchanged

- 3 (c)
The wavelength of X-ray lines is given by Rydberg

$$\text{Formula } \frac{1}{\lambda} = RZ^2 \left(\frac{1}{n_1^2} - \frac{1}{n_2^2} \right)$$

For K_α line, $n_1 = 1$ and $n_2 = 2$

$$\begin{aligned} \therefore \frac{1}{\lambda} &= RZ^2 \left(\frac{3}{4} \right) \Rightarrow Z = \left(\frac{4}{3R\lambda} \right)^{1/2} \\ &= \left[\frac{4}{3(1.097 \times 10^7 \text{m}^{-1})(0.76 \times 10^{-10} \text{m})} \right]^{1/2} = 39.99 \approx 40 \end{aligned}$$

- 4 (d)
 $\Delta\lambda = \lambda_{K_\alpha} - \lambda_{\min}$ When V is halved λ_{\min} becomes two time but λ_{K_α} remains the same.
 $\therefore \Delta\lambda' = \lambda_{K_\alpha} - 2\lambda_{\min} = 2(\Delta\lambda) - \lambda_{K_\alpha}$
 $\therefore \Delta\lambda' < 2(\Delta\lambda)$

- 5 (c)
X-rays are electromagnetic waves of wavelength ranging from 0.1 to 100Å

- 6 (d)
 $qE = mg \quad \dots(i)$
 $6\pi\eta rv = mg$
 $\frac{4}{3}\pi r^3 \rho g = mg \quad \dots(ii)$
 $\therefore r = \left(\frac{3mg}{4\pi\rho g} \right)^{1/3} \quad \dots(iii)$

Substituting the value of r in Eq. (ii), we get

$$6\pi\eta v \left(\frac{3mg}{4\pi\rho g}\right)^{1/3} = mg$$

or $(6\pi\eta v)^3 \left(\frac{3mg}{4\pi\rho g}\right) = (mg)^3$

Again substituting $mg = qE$, we get

$$(qE)^2 = \left(\frac{3}{4\pi\rho g}\right)(6\pi\eta v)^3$$

Or $qE = \left(\frac{3}{4\pi\rho g}\right)^{1/2} (6\pi\eta v)^{3/2}$

$$\therefore q = \frac{1}{E} \left(\frac{3}{4\pi\rho g}\right)^{1/2} (6\pi\eta v)^{3/2}$$

Substituting the values, we get

$$q = \frac{7}{81\pi \times 10^5} \sqrt{\frac{3}{4\pi \times 900 \times 9.8} \times 216\pi^3} \times \sqrt{(1.8 \times 10^{-5} \times 2 \times 10^{-3})^3} = 8.0 \times 10^{-19} \text{ C}$$

7 **(c)**

$$K.E. = 2E_0 - E_0 = E_0 \text{ (for } 0 \leq x \leq 1) \Rightarrow \lambda_1 = \frac{h}{\sqrt{2mE_0}}$$

$$K.E. = 2E_0 \text{ (for } x > 1) \Rightarrow \lambda_2 = \frac{h}{\sqrt{4mE_0}} \Rightarrow \frac{\lambda_1}{\lambda_2} = \sqrt{2}$$

8 **(c)**

Among the given metals, aluminium thermionically emits an electron at a relatively lowest temperature

9 **(c)**

Speed obtained by the particle after falling through a potential difference of V volt is

$$v_A = \sqrt{\frac{2Vq}{m}} \dots (i)$$

And $v_B = \sqrt{\frac{2V \times 4q}{m}} \dots (ii)$

Now dividing Eq. (i) by Eq. (ii), we get

$$\frac{v_A}{v_B} = \sqrt{\frac{1}{4}} = \frac{1}{2}$$

So, $v_A : v_B = 1 : 2$

10 **(a)**

$$\frac{u_1}{u_2} = \frac{1}{2}$$

Accelerations of cathode rays in electric field, $\vec{a} = \frac{eE}{m}$

It is same for both the cathode rays

As displacement, $s = ut + \frac{1}{2}at^2$

So for a given value of a and t , $s \propto u$

$$\text{So, } \frac{s_1}{s_2} = \frac{u_1}{u_2} = \frac{1}{2}$$

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(b)

Here, $\lambda_0 = 200\text{nm}$; $\lambda = 100\text{nm}$;

$hc/e = 1240\text{eV nm}$

maximum KE = $\frac{hc}{\lambda e} - \frac{hc}{\lambda_0 e}$ (in eV)

$$= \frac{hc}{e} \left(\frac{1}{\lambda} - \frac{1}{\lambda_0} \right)$$

$$= 1240 \left(\frac{1}{100} - \frac{1}{200} \right)$$

$$= 6.2 \text{ eV}$$

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(c)

According to J. J. Thomson's cathode ray tube experiment the e/m of electrons is much greater than the e/m of protons.

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(b)

Maximum KE = $\frac{hc}{\lambda} - \phi_0$

$$= \frac{6.6 \times 10^{-34} \times 3 \times 10^8}{400 \times 10^{-10}} \times \frac{1}{1.6 \times 10^{-19}} - 2 = 1.1 \text{ eV}$$

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(c)

$\lambda = \frac{h}{\sqrt{2mE}} = \frac{h}{\sqrt{2m} \cdot \sqrt{E}}$. Taking log of both sides

$$\log \lambda = \log \frac{h}{\sqrt{2m}} + \log \frac{1}{\sqrt{E}} \Rightarrow \log \lambda = \log \frac{h}{\sqrt{2m}} - \frac{1}{2} \log E$$

$$\Rightarrow \log \lambda = -\frac{1}{2} \log E + \log \frac{h}{\sqrt{2m}}$$

This is the equation of straight line having slope $(-1/2)$ and positive intercept on $\log \lambda$ axis

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(b)

Cut-off wavelength depends on the applied voltage not on the atomic number of the target. Characteristic wavelengths depends on the atomic number of target.

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(c)

For k_α emission

transition L shell to k - shell

For k_β emission

transition M shell to k - shell

For L_α emission

transition M shell to L - shell

$$E_M - E_K = (E_M - E_L) + (E_L - E_K)$$

$$\Rightarrow hf_2 = hf_3 + hf_1 \Rightarrow f_2 = f_1 + f_3$$

18 **(a)**

Number of photons emitted per second

$$n = \frac{p}{hv} = \frac{10 \times 10^3}{6.6 \times 10^{-34} \times 880 \times 10^3} = 1.72 \times 10^{31}$$

19 **(a)**

$$p = \frac{h}{\lambda} = \frac{6.6 \times 10^{-34}}{4400 \times 10^{-10}} = 1.5 \times 10^{-27} \text{ kg.m/s}$$

$$\text{and mass } m = \frac{p}{c} = \frac{1.5 \times 10^{-27}}{3 \times 10^8} = 5 \times 10^{-36} \text{ kg}$$

20 **(a)**

$$\lambda = \frac{h}{p} = \frac{h}{mv}$$

PE

ANSWER-KEY										
Q.	1	2	3	4	5	6	7	8	9	10
A.	A	B	C	D	C	D	C	C	C	A
Q.	11	12	13	14	15	16	17	18	19	20
A.	B	C	D	B	C	B	C	A	A	A

PE