Class: XIIth
Date :

## Solutions

## Subject : PHYSICS

DPP No. : 1

## Topic :-Atoms

1
(b)

As $\quad E_{1}>E_{2}$
$\therefore \quad v_{1}>v_{2}$
$i e$, photon oh higher frequency will be emitted if transition takes place from $n=2$ to $n=1$.
2
(b)

Radius of Bohr orbit is given by

$$
r_{n}=\left(\frac{\varepsilon_{0} h^{2}}{\pi m e^{2}}\right) n^{2}
$$

The quantities in the bracket are constant

$$
\therefore \quad r_{n} \propto n^{2}
$$

The expression gives the radius of the nth Bohr orbit

$$
\begin{aligned}
\frac{r_{1}}{r_{2}} & =\frac{n_{1}^{2}}{n_{2}^{2}} \\
\frac{a}{r_{2}} & =\frac{1}{3^{2}} \\
r_{2} & =9 a
\end{aligned}
$$

(b)

The energy taken by hydrogen atom corresponds to its transition from
$n=1$ to $n=3$ state.
$\Delta E$ (given to hydrogen atom)

$$
\begin{aligned}
& =13.6\left(1-\frac{1}{9}\right) \\
& =13.6 \times \frac{8}{9}=12.1 \mathrm{eV}
\end{aligned}
$$

(b)

Energy released $=E_{4}-E_{1}$
$=-\frac{13.6}{4^{2}}-\left(-\frac{13.6}{1^{2}}\right)=1.75 \mathrm{eV}$
(c)

The excitation energy in the first excited state is

$$
\begin{array}{cc} 
& E=R h c Z^{2}\left(\frac{1}{1^{2}}-\frac{1}{2^{2}}\right)=(13.6 \mathrm{eV}) \times Z^{2} \times \frac{3}{4} \\
\therefore & 40.8=13.6 \times Z^{2} \times \frac{3}{4} \\
\Rightarrow & Z=2
\end{array}
$$

So, the ion in problem is $\mathrm{He}^{+}$. The energy of the ion in the ground state is
$E=\frac{R h c Z^{2}}{1^{2}}=13.6 \times 4=54.4 \mathrm{eV}$
Hence, 54.4 eV is required to remove the electron from the ion.
(b)

Ultraviolet region Lyman series
Visible region Balmer series
Infrared region Paschen series, Brackett series
Pfund series
From the above chart it is clear that Balmer series lies in the visible region of the electromagnetic spectrum.
(b)

At distance of closest approach relative velocity of two particles is $v$. Here target is considered as stationary, so $\alpha$-particle comes to rest instantaneously at distance of closest approach. Let required distance is $r$, then from work energy-theorem.

$$
\begin{aligned}
0-\frac{m v^{2}}{2} & =-\frac{1}{4 \pi \varepsilon_{0}} \frac{Z_{e} \times Z_{e}}{r} \\
r & \propto \frac{1}{m} \\
& \propto \frac{1}{v^{2}} \\
& \propto Z e^{2}
\end{aligned}
$$

(a)

As $r \propto n^{2}$, therefore, radius of 2nd Bohr's orbit $=4 a_{0}$
(b)
$\mathrm{KE}=\frac{1}{2} \frac{e^{2}}{r}$
(a)
$E=-Z^{2} \frac{13.6}{n^{2}} \mathrm{eV}$
For first excited state,

$$
\begin{aligned}
E_{2} & =-3^{2} \times \frac{13.6}{4} \\
& =-30.6 \mathrm{eV}
\end{aligned}
$$

Ionisation energy for first excited state of $\mathrm{Li}^{2+}$ is 30.6 eV .
(a)

For maximum wavelength of Balmer series

$$
\begin{equation*}
\frac{1}{\lambda_{\max }}=R\left(\frac{1}{2^{2}}-\frac{1}{3^{2}}\right)=\frac{R \times 5}{36} \tag{i}
\end{equation*}
$$

For minimum wavelength of Balmer series,

$$
\begin{equation*}
\frac{1}{\lambda_{\min }}=R\left(\frac{1}{2^{2}}-\frac{1}{\infty}\right)=\frac{R}{4} \tag{ii}
\end{equation*}
$$

From Eqs.(i)and (ii), we have

$$
\therefore \quad \frac{\lambda_{\min }}{\lambda_{\max }}=\frac{R \times 5}{36} \times \frac{4}{R}=\frac{5}{9}
$$

(a)

Frequency, $\quad v=R C\left[\frac{1}{n_{1}^{2}}-\frac{1}{n_{2}^{2}}\right]$

$$
v_{1}=R C\left[1-\frac{1}{\infty}\right]=R C
$$

$$
v_{2}=R C\left[1-\frac{1}{4}\right]=\frac{3}{4} R C
$$

$$
v_{3}=R C\left[\frac{1}{4}-\frac{1}{\infty}\right]=\frac{R C}{4}
$$

$$
\Rightarrow \quad \mathrm{v}_{1}-\mathrm{v}_{2}=\mathrm{v}_{3}
$$

(b)

Time period of electron, $\mathrm{T}=\frac{4 \varepsilon_{0}^{2} n^{3} h^{3}}{m Z^{2} e^{4}}$

$$
\begin{array}{lr}
\therefore & T \propto n^{3} \\
\therefore & \frac{1}{\text { frequency }(f)} \propto n^{3} \\
\text { or } & f \propto n^{-3}
\end{array}
$$

(a)
$E=E_{2}-E_{1}=-\frac{13.6}{2^{2}}-\left(-\frac{13.6}{1^{2}}\right)=10.2 \mathrm{eV}$
(a)
$\frac{1}{\lambda_{\text {min }}}=R\left[\frac{1}{2^{2}}-\frac{1}{3^{2}}\right]=\frac{R \times 5}{36}$
$\frac{1}{\lambda_{\text {max }}}=R\left[\frac{1}{2^{2}}-\frac{1}{\infty}\right]=\frac{R}{4}$
$\frac{\lambda_{\text {min }}}{\lambda_{\text {max }}}=\frac{R \times 5}{36} \times \frac{4}{R}=\frac{5}{9}$
(d)

Radius of orbit of electron in $n$th excited state of hydrogen

$$
\begin{array}{ll} 
& r=\frac{\varepsilon_{0} h^{2} n^{2}}{\pi m Z e^{2}} \\
\therefore & r \propto \frac{n^{2}}{Z} \\
\therefore & \frac{r_{1}}{r_{2}}=\frac{n_{1}^{2}}{n_{2}^{2}} \times \frac{Z_{2}}{Z_{1}} \\
\text { But } & r_{1}=r_{2} \\
\text { So, } & n_{2}^{2}=n_{1}^{2} \times \frac{Z_{2}}{Z_{1}}
\end{array}
$$

Here,
$n_{1}=1$ (ground state of hydrogen),
$Z_{1}=1$ (atomic number of hydrogen),
$Z_{2}=4$ (atomic number of beryllium)

$$
\begin{array}{lll}
\therefore & \sqrt{n_{2}^{2}} & =(1)^{2} \times \frac{4}{1} \\
\text { or } & & n_{2}^{2} \\
\text { or } & n_{2} & =2
\end{array}
$$

(a)

For spin-orbit interaction, only the case ofl $\geq 1$ is important since spin orbit interaction vanishes for $l=0$.
(b)

Hydrogen atom normally stays in lowest energy state ( $n=1$ ), where its energy is

$$
E_{1}=\frac{R h c}{1^{2}}=-R h c
$$

On being ionized its energy becomes zero. Thus, ionization of hydrogen atom is

$$
\begin{aligned}
& =\text { energy after ionisation }- \text { energy before ionisation } \\
& =0-(-R h c)=R h c \\
& =\left(1.097 \times 10^{7} \mathrm{~m}^{-1}\right)(6.63 \times 10-34 \mathrm{~J}-\mathrm{s})\left(3 \times 108 \mathrm{~ms}^{-1}\right) \\
& =21.8 \times 10^{-19} \mathrm{~J} \\
& =\frac{21.8 \times 10^{-19}}{1.6 \times 10^{-19}}=13.6 \mathrm{eV}
\end{aligned}
$$

(d)

In ground state $\mathrm{TE}=-13.6 \mathrm{eV}$
In first excited state, $\mathrm{TE}=-3.4 \mathrm{eV}$, $i e$,
10.2 eV above the ground state.

If ground state energy is taken as zero, the total energy in
First excited state $=10.2 \mathrm{eV}$

| ANSWER-KEY |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Q. | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |  |  |
| A. | B | B | B | B | C | B | B | A | B | A |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| Q. | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |  |  |
| A. | A | A | B | A | A | D | A | D | B | D |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |



