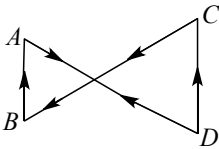


Topic :- Alternating current

1 (d)

As the magnetic field directed into the paper is increasing at a constant rate, therefore, induced current should produce a magnetic field directed out of the paper. Thus current in both the loops must be anti-clock-wise.



As area of loop on right side is more, therefore, induced emf of right side of loop will be more compared to the emf induced on the left-side of the loop

$$\left[\therefore e = -\frac{d\phi}{dt} = -A \frac{dB}{dt} \right]$$

2 (b)

Given, $L = 30 \text{ mH}$

$$V_{rms} = 220 \text{ V}$$

$$f = 50 \text{ Hz}$$

Now, $X_L = \omega L = 2\pi fL$

$$= 2 \times 3.14 \times 50 \times 30 \times 10^{-3}$$

$$= 9.42 \Omega$$

The rms current in the coil is

$$i_{rms} = \frac{V_{rms}}{X_L} = \frac{220 \text{ V}}{9.42 \Omega} = 23.4 \text{ A}$$

3 (c)

$$P = V_{r.m.s.} \times i_{r.m.s.} \times \cos \phi = \frac{100}{\sqrt{2}} \times \frac{100 \times 10^{-3}}{\sqrt{2}} \times \cos \frac{\pi}{3}$$

$$= \frac{10^4 \times 10^{-3}}{2} \times \frac{1}{2} = \frac{10}{4} = 2.5 \text{ watt}$$

4

(d)

Initial flux linked with inner coil when $i = 0$ is zero. Final flux linked with inner coil when

$$i = i \text{ is } \left(\frac{\mu_0 i}{2\pi b}\right) \pi a^2$$

$$\therefore \text{Change in flux, } d\phi = \left(\frac{\mu_0 i}{2\pi b}\right) \pi a^2$$

$$\text{As } dq = \frac{d\phi}{R}$$

\therefore Total charge circulating the inner coil is

$$= \left(\frac{\mu_0 i}{2\pi b}\right) \frac{\pi a^2}{R} = \frac{\mu_0 i a^2}{2 R b}$$

5

(a)

Induced emf produced in coil

$$e = \frac{-d\phi}{dt} = \frac{-d}{dt}(BA)$$

$$\therefore |e| = A \frac{dB}{dt} = 0.01 \times \frac{1}{1 \times 10^{-3}}$$

$$|e| = 10 \text{ V}$$

Current produced in coil,

$$i = \frac{|e|}{R} = \frac{10}{2} = 5 \text{ A}$$

Heat evolved = $i^2 R t$

$$= (5)^2 \times (2) \times 1 \times 10^{-3} = 0.05 \text{ J}$$

6

(c)

Power = Rate of work done in one complete cycle.

$$\text{or } P_{av} = \frac{W}{T}$$

$$\text{or } P_{av} = \frac{(E_0 I_0 \cos \phi) T / 2}{T}$$

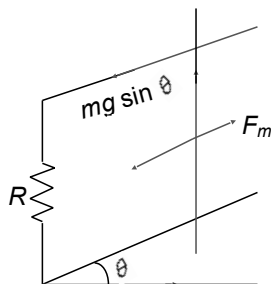
$$\text{or } P_{av} = \frac{E_0 I_0 \cos \phi}{2}$$

Where $\cos \phi$ is called the power factor of an AC circuit.

7

(c)

Terminal velocity of the rod is attained when magnetic force on the rod (Bil) balances the component of weight of the rod ($mg \sin \theta$), figure.



$$\text{ie, } Bil = mg \sin \theta$$

$$B \left(\frac{e}{R}\right) l = mg \sin \theta$$

$$\frac{Bl}{R}(e) = mg \sin \theta$$

$$\frac{Bl}{R}(Blv_r) = mg \sin \theta$$

$$r_T = \frac{mg R \sin \theta}{B^2 l^2}$$

8 (a)

$$X_C = \frac{1}{2\pi\nu C} \Rightarrow C = \frac{1}{2\pi\nu X_C} = \frac{1}{2 \times \pi \times \frac{400}{\pi} \times 25} = 50 \mu F$$

10 (c)

Here, $M = 2H$, $d\phi = 4 \text{ Wb}$, $dt = 10 \text{ s}$

As $\phi = M i$

$$d\phi = M di$$

$$\text{Or } di = \frac{d\phi}{M} = \frac{4}{2} = 2 \text{ A}$$

$$\text{Also, } d\phi = M (di) = 2(1) \\ = 2 \text{ Wb}$$

11 (a)

$$\tan \phi = \frac{X_L}{R} = \frac{\sqrt{3} R}{R} = \sqrt{3} \Rightarrow \phi = 60^\circ = \pi/3$$

12 (c)

$$\text{Time difference} = \frac{T}{2\pi} \times \phi = \frac{(1/50)}{2\pi} \times \frac{\pi}{4} = \frac{1}{400} \text{ s} = 2.5 \text{ m-s}$$

13 (a)

Here, Resistance, $R = 3\Omega$

Inductive reactance, $X_L = 10\Omega$

Capacitive reactance, $X_C = 14\Omega$

The impedance of the series LCR circuit is

$$Z = \sqrt{R^2 + (X_C + X_L)^2} = \sqrt{(3)^2 + (14 - 10)^2}$$

$$Z = 5\Omega$$

14 (d)

In purely inductive circuit voltage leads the current by 90°

15 (a)

Q factor is given by $\frac{1}{R} \sqrt{\frac{L}{C}}$

So, for large quality factor the inductance should be large and resistance and capacitance must be small

16 **(b)**

$$\begin{aligned}\text{As, power factor} &= \frac{\text{true power}}{\text{apparent power}} \\ &= \cos \phi \\ &= \frac{R}{\sqrt{R^2 + (X_L - X_C)^2}}\end{aligned}$$

$$\therefore \text{power factor} = \cos \phi = \frac{R}{Z}$$

In a non-inductive circuit, $X_L = X_C$

$$\therefore \text{Power factor} = \cos \phi = \frac{R}{\sqrt{R^2}} = \frac{R}{R} = 1$$

$$\therefore \phi = 0^\circ$$

This is the maximum value of power factor. In a pure inductor or an ideal capacitor

$$\phi = 90^\circ$$

$$\therefore \text{Power factor} = \cos \phi = \cos 90^\circ = 0$$

Average power consumed in a pure inductor or ideal capacitor

$$P = E_v \cdot I_v \cos 90^\circ = \text{zero}$$

Therefore, current through pure L or pure C , which consumes no power for its maintenance in the circuit is called ideal current or wattless current.

17 **(d)**

Potential difference across the capacitor = emf induced across $HE = Blv$ which is constant. Therefore, charge stored in the capacitor is constant. Hence current in the circuit $HKDE$ is zero.

18 **(b)**

$$e = -L \frac{dI}{dt} = -5 \times (-2) = +10 \text{ V}$$

19 **(b)**

$$\text{Resistance of a bulb} = \frac{(\text{Rated voltage})^2}{\text{Rated power}}$$

$$= \frac{(220)^2}{100} = 484 \Omega$$

$$\text{Peak voltage of the source, } V_0 = 220\sqrt{2} \text{ V} = 311 \text{ V}$$

20 **(a)**

As $M = \frac{\mu_0 N_1 N_2 A}{l}$, therefore, M becomes 4 times

| ANSWER-KEY | | | | | | | | | | |
|-------------------|----|----|----|----|----|----|----|----|----|----|
| Q. | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| A. | D | B | C | D | A | C | C | A | A | C |
| | | | | | | | | | | |
| Q. | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| A. | A | C | A | D | A | B | D | B | B | A |
| | | | | | | | | | | |

P E