

**Topic :- Alternating current**

1 (c)

Power remains constant in a ideal step down transformer.

2 (b)

$$V = 50 \times 2 \sin 100\pi t \cos 100\pi t = 50 \sin 200\pi t$$
$$\Rightarrow V_0 = 50 \text{ volts and } \nu = 100\text{Hz}$$

3 (b)

Capacitive reactance is given by

$$X_C = \frac{1}{\omega C}$$

Where  $C$  is capacitance and  $\omega$  the angular frequency ( $\omega = 2\pi f$ ).

$$\therefore X_C = \frac{1}{2\pi f C}$$

$$\Rightarrow X_C \propto \frac{1}{f}$$

Hence, when frequency  $f$  increases capacitive reactance decreases.

4 (a)

$$\text{Power factor} = \cos \phi = \frac{R}{Z}$$
$$= \frac{12}{15} = \frac{4}{5} = 0.8$$

5 (d)

$$\text{Given } \omega L = \frac{1}{\omega C} \Rightarrow \omega^2 = \frac{1}{LC}$$

$$\text{Or } \omega = \frac{1}{\sqrt{10^{-3} \times 10 \times 10^{-6}}} = \frac{1}{\sqrt{10^{-8}}} = 10^4$$

$$X_L = \omega L = 10^4 \times 10^{-3} = 10 \Omega$$

6 (b)

$$i_s = \frac{E_s}{Z} = \frac{22}{220} = 0.1 \text{ A}$$

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**(a)**

The instantaneous value of voltage is

$$E = 100 \sin(100t) \text{ V} \quad \dots(i)$$

Compare it with  $E = E_0 \sin(\omega t) \text{ V}$

We get

$$E_0 = 100 \text{ V}, \omega = 100 \text{ rad s}^{-1}$$

The rms value of voltage is

$$E_{rms} = \frac{E_0}{\sqrt{2}} = \frac{100}{\sqrt{2}} \text{ V} = 70.7 \text{ V}$$

The instantaneous value of current is

$$I = 100 \sin\left(100t + \frac{\pi}{3}\right) \text{ mA}$$

Compare it with

$$I = I_0 \sin(\omega t + \phi)$$

We get

$$I_0 = 100 \text{ mA}, \omega = 100 \text{ rad s}^{-1}$$

The rms value of current is

$$I_{rms} = \frac{I_0}{\sqrt{2}} = \frac{100}{\sqrt{2}} \text{ mA} = 70.7 \text{ mA}$$

8

**(a)**

$$\text{Resistance, } R = \frac{100}{10} = 10 \, \Omega$$

$$\text{Inductive reactance, } X_L = 2\pi fL$$

$$\frac{100}{8} = 2\pi \times 50 \times L$$

$$\Rightarrow L = \frac{1}{8\pi} \text{ H}$$

$$X'_L = 2\pi f' L = 2\pi \times 40 \times \frac{1}{8\pi} = 10 \, \Omega$$

$$\text{Impedance of the circuit is } Z = \sqrt{R^2 + X'_L{}^2}$$

$$= \sqrt{(10)^2 + (10)^2}$$

$$= 10\sqrt{2} \, \Omega$$

$$\text{Current in the circuit is } i = \frac{V}{Z} = \frac{150}{10\sqrt{2}} = \frac{15}{\sqrt{2}} \text{ A}$$

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**(a)**

$$\because (X_C) \gg (X_L)$$

10

**(a)**

$$i_{rms} = \frac{200}{280} = \frac{5}{7} \text{ A. So } i_0 = i_{rms} \times \sqrt{2} = \frac{5}{7} \times \sqrt{2} \approx 1 \text{ A}$$

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**(d)**

In series  $L - R$  circuit, impedance is given by

$$Z = \sqrt{R^2 + X_L^2}$$

Where  $R$  is the resistance and  $X_L$  the inductive reactance.

$$\begin{aligned} \text{Given, } R &= 8\Omega, X_L = 6\Omega \\ \therefore Z &= \sqrt{(8)^2 + (6)^2} \\ &= \sqrt{64 + 36} \\ &= \sqrt{100} = 10\Omega \end{aligned}$$

14 **(a)**

If the current is wattless then power is zero. Hence phase difference  $\phi = 90^\circ$

15 **(a)**

In  $LCR$  circuit; in the condition of resonance  $X_L = X_C$ , i.e., circuit behaves as resistive circuit. In resistive circuit power factor is maximum

16 **(c)**

$$\begin{aligned} I_{av} &= \frac{\int_0^{T/2} i dt}{\int_0^{T/2} dt} = \frac{\int_0^{T/2} I_0 \sin(\omega t) dt}{T/2} \\ &= \frac{2I_0}{T} \left[ -\frac{\cos \omega t}{\omega} \right]_0^{T/2} = \frac{2I_0}{T} \left[ -\frac{\cos\left(\frac{\omega T}{2}\right)}{\omega} + \frac{\cos 0^\circ}{\omega} \right] \\ &= \frac{2I_0}{\omega T} [-\cos \pi + \cos 0^\circ] = \frac{2I_0}{2\pi} [1 + 1] = \frac{2I_0}{\pi} \end{aligned}$$

17 **(c)**

At resonance,  $\omega L = \frac{1}{\omega C}$

Current flowing through the circuit,

$$\begin{aligned} I &= \frac{V_R}{R} \\ &= \frac{100}{1000} = 0.1 \text{ A} \end{aligned}$$

So, voltage across  $L$  is given by

$$V_L = IX_L = I\omega L$$

But  $\omega L = \frac{1}{\omega C}$

$$\begin{aligned} \therefore V_L &= \frac{1}{\omega C} \\ &= \frac{0.1}{200 \times 2 \times 10^{-6}} = 250 \text{ V} \end{aligned}$$

18 **(b)**

When the direction of current is reversed, moving from  $B$  to  $A$ .

$$V_B - V_A = [5 \times 10^{-3}(-10^3) + 15 + 1 \times 5]$$

$$= 15 \text{ volt}$$

19 **(b)**

The instantaneous voltage through the given device

$$e = 80 \sin 100\pi t$$

Comparing the given instantaneous voltage with standard instantaneous voltage

$$e = e_0 \sin \omega t.$$

We get  $e_0 = 80 \text{ V}$

Where  $e_0$  is the peak value of voltage

Impedance ( $Z$ ) =  $20\Omega$

$$\begin{aligned} \text{Peak value of current } I_0 &= \frac{e_0}{Z} \\ &= \frac{80}{20} = 4\text{A} \end{aligned}$$

Effective value of current (root mean square value of current).

$$\begin{aligned} I_{rms} &= \frac{I_0}{\sqrt{2}} \\ &= \frac{4}{\sqrt{2}} = 2\sqrt{2} = 2.828 \text{ A} \end{aligned}$$

20 **(b)**

$$\text{Charging current, } I = \frac{E}{R} e^{-\frac{t}{RC}}$$

Taking log both sides,

$$\text{Log } I = \log \left( \frac{E}{R} \right) - \frac{t}{RC}$$

When  $R$  is doubled, slope of curve increases. Also at  $t = 0$ , the current will be less. Graph  $Q$  represents the best.

ANSWER-KEY										
Q.	1	2	3	4	5	6	7	8	9	10
A.	C	B	B	A	D	B	A	A	A	A
Q.	11	12	13	14	15	16	17	18	19	20
A.	D	D	C	A	A	C	C	B	B	B

PE