

Topic :- Alternating current

1 (d)

$$i = \frac{220}{\sqrt{(20)^2 + (2 \times \pi \times 50 \times 0.2)^2}} = \frac{220}{66} = 3.33 \text{ A}$$

2 (a)

$$E_s = \frac{n_s}{n_p} E_p = \frac{4200}{2100} \times 120 = 240 \text{ V}$$
$$i_s = \frac{n_s}{n_p} i_p = \frac{2100}{4200} \times 10 = 5 \text{ A}$$

3 (b)

$$i_{r.m.s.} = \frac{i_0}{\sqrt{2}} = \frac{4}{\sqrt{2}} = 2\sqrt{2} \text{ ampere}$$

4 (a)

As the current i leads the emf e by $\frac{\pi}{4}$, it is an $R - C$ circuit

$$\tan \phi = \frac{X_C}{R}$$

or $\tan \frac{\pi}{4} = \frac{1}{\omega C R}$

$$\therefore \omega C R = 1$$

As $\omega = 100 \text{ rads}^{-1}$

The product of $C - R$ should be $\frac{1}{100} \text{ s}^{-1}$.

5 (d)

Phase angle $\phi = 90^\circ$, so power $P = V \cos \phi = 0$

6 (d)

Current lags the voltage if $\omega L > \frac{1}{\omega C}$

$$f > \frac{1}{2\pi\sqrt{LC}} \Rightarrow f > f_r$$

7 (c)

$$v = \frac{\omega}{2\pi} = \frac{120 \times 7}{2 \times 22} = 19 \text{ Hz}$$

$$V_{r.m.s.} = \frac{240}{\sqrt{2}} = 120\sqrt{2} = 170 \text{ V}$$

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(c)For an $R - C$ circuit

$$\text{Applied voltage, } V = \sqrt{V_R^2 + V_C^2}$$

$$\therefore 50 = \sqrt{(40)^2 + V_C^2}$$

$$\Rightarrow V_C = 30 \text{ V}$$

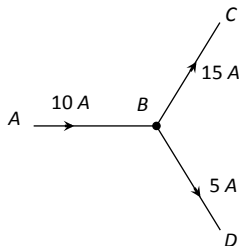
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(d)

Power factor

$$\begin{aligned} \cos \phi &= \frac{R}{\sqrt{R^2 + \omega^2 L^2}} \\ &= \frac{30}{\sqrt{(30)^2 + (100)^2 \times (400 \times 10^{-3})^2}} \\ &= \frac{30}{\sqrt{900 + 1600}} = \frac{30}{50} = 0.6 \end{aligned}$$

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(a)Yes, in AC if branch AB has R , BC has a capacitor C , and BD has a pure inductance L 

P

E

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(c)At $A : X_C > X_L$ At $B : X_C = X_L$ At $C : X_C < X_L$

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(c)

Here: Current in the circuit

$$(i) = 15 \text{ mA} = 15 \times 10^{-3} \text{ A}$$

Resistance $R = 4000 \text{ Volt}$ Applied voltage in the circuit = 240 V At any instant, the *emf* of the battery is equal to the sum of potential drop on the resistor and the *emf* developed in the induction coil

$$\text{Hence, } E = iR + L \frac{di}{dt}$$

$$240 = 15 \times 10^{-3} \times 4000 + L \frac{di}{dt}$$

$$\text{Hence, } L \frac{di}{dt} = 240 - 60 = 180 \text{ V}$$

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(b) L/R represents time constant of $R-L$ circuit. Therefore, its dimensions are $[M^0 L^0 T^1]$.

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(a)This is a parallel circuit, For oscillation, the energy in L and C will be alternately maximum

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(a)

The current in a coil is given by

$$i = i_0 e^{-t/\tau}$$

Now, $i = \frac{i_0}{\eta}$ in $t = t_0$

$$\therefore \frac{i_0}{\eta} = i_0 e^{-t_0/\tau}$$

$$e^{-t_0/\tau} = \eta^{-1}$$

Taking log of both sides,

$$-\frac{t_0}{\tau} \log_e e = -1 \log_e \eta$$

$$\frac{t_0}{\tau} = \log_e \eta$$

$$\tau = t_0 / \log_e \eta = t_0 / \ln \eta$$

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(b)

Since voltage is lagging behind the current, so there must be no inductor in the box

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(b)

Average power dissipated in an AC circuit

$$P_{av} = V_{rms} I_{rms} \cos \phi \quad \dots(i)$$

Where the term $\cos \phi$ is known as power factor.Given, $V_{rms} = 100 \text{ V}$, $R = 100 \Omega$, $\phi = 30^\circ$

$$\therefore I_{rms} = \frac{V_{rms}}{R} = \frac{100}{100} = 1 \text{ A}$$

Putting the values in Eq. (i), we get

$$P_{av} = 100 \times 1 \times \cos 30^\circ$$

$$= 100 \frac{\sqrt{3}}{2}$$

$$= 50\sqrt{3} = 86.6 \text{ W}$$

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(c)

$$\tan \phi = \frac{\omega L - \frac{1}{\omega C}}{R}$$

 ϕ being the angle by which the current leads the voltage.Given, $\phi = 45^\circ$

$$\therefore \tan 45^\circ = \frac{\omega L - \frac{1}{\omega C}}{R}$$

$$\Rightarrow 1 = \frac{\omega L - \frac{1}{\omega C}}{R}$$

$$\Rightarrow R = \omega L - \frac{1}{\omega C}$$

$$\Rightarrow C = \frac{1}{\omega(\omega L - R)}$$

$$= \frac{1}{2\pi f(2\pi fL - R)}$$

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(d)In an $L - C - R$ circuit in resonance condition

$$X_L = X_C \quad \text{or} \quad X_C - X_L = 0$$

ANSWER-KEY										
Q.	1	2	3	4	5	6	7	8	9	10
A.	D	A	B	A	D	D	C	C	D	A
Q.	11	12	13	14	15	16	17	18	19	20
A.	C	C	B	A	A	B	B	C	C	D

PE