

Topic :- TRIGONOMETRIC FUNCTIONS

1. If $\theta \in [0, 5\pi]$ and $r \in R$ such that $2\sin \theta = r^4 - 2r^2 + 3$, then the maximum number of values of the pair (r, θ) is
 a) 6 b) 8 c) 10 d) None of these
2. In a triangle ABC , $r =$
 a) $(s - a)\tan \frac{B}{2}$ b) $(s - b)\tan \frac{B}{2}$ c) $(s - b)\tan \frac{C}{2}$ d) $(s - a)\tan \frac{C}{2}$
3. If p_1, p_2, p_3 are altitude of a triangle ABC from the vertices A, B, C and Δ , the area of the triangle, then $\frac{1}{p_1^2} + \frac{1}{p_2^2} + \frac{1}{p_3^2} =$
 a) $\frac{\cot A + \cot B + \cot C}{\Delta}$
 b) $\frac{\Delta}{\cot A + \cot B + \cot C}$
 c) $\Delta(\cot A + \cot B + \cot C)$
 d) None of these
4. Number of solutions of the equation $\sin 2\theta + 2 = 4 \sin \theta + \cos \theta$ lying in the interval $[\pi, 5\pi]$, is
 a) 0 b) 2 c) 4 d) 5
5. If twice the square of the diameter of a circle is equal to half the sum of the squares of the sides of inscribed triangle ABC , then $\sin^2 A + \sin^2 C$ is equal to
 a) 1 b) 2 c) 4 d) 8
6. $\tan 9^\circ - \tan 27^\circ - \tan 63^\circ + \tan 81^\circ$ is equal to
 a) 0 b) 1 c) -1 d) 4
7. If $\sin 4A - \cos 2A = \cos 4A - \sin 2A$, ($0 < A < \frac{\pi}{4}$), then the value of $\tan 4A$ is
 a) 1 b) $\frac{1}{\sqrt{3}}$ c) $\sqrt{3}$ d) $\frac{\sqrt{3}-1}{\sqrt{3}+1}$
8. In a ΔABC , $\sin A$ and $\sin B$ are the roots of the equation $c^2x^2 - c(a+b)x + ab = 0$, then $\sin C =$
 a) $1/\sqrt{2}$ b) $1/2$ c) 1 d) 0
9. If $\sin(\alpha + \beta) = 1, \sin(\alpha - \beta) = 1/2; \alpha, \beta \in [0, \pi/2]$, then $\tan(\alpha + 2\beta)\tan(2\alpha + \beta)$ is equal to
 a) 1 b) -1 c) 0 d) $1/2$
10. If $a_{n+1} = \sqrt{\frac{1}{2}(1 + a_n)}$, then $\cos\left(\frac{\sqrt{1-a_0^2}}{a_1 a_2 a_3 \dots \text{to } \infty}\right) =$
 a) 1 b) -1 c) a_0 d) $1/a_0$
11. If the angles of a triangle are in the ratio $1 : 2 : 7$, then the ratio of the greatest side to the least side is
 a) $(\sqrt{5} - 1) : (\sqrt{5} + 1)$ b) $(\sqrt{5} + 1) : (\sqrt{5} - 1)$ c) $(\sqrt{5} + 2) : (\sqrt{5} - 2)$ d) $(\sqrt{5} - 2) : (\sqrt{5} + 2)$

12. In a ΔABC , $A = \frac{2\pi}{3}$, $b - c = 3\sqrt{3}$ cm and $\Delta = \frac{9\sqrt{3}}{2}$ cm². Then, $a =$
- a) $6\sqrt{3}$ cm b) 9 cm c) 18 cm d) 12 cm
13. If the radius of the incircle of a triangle with its sides $5k, 6k$, and $5k$ is 6, then k is equal to
- a) 3 b) 4 c) 5 d) 6
14. The minimum value of $2^{\sin x} + 2^{\cos x}$, is
- a) 1 b) 2 c) $2^{\frac{1}{\sqrt{2}}}$ d) $2^{1-\frac{1}{\sqrt{2}}}$
15. Minimum value of $\frac{1}{3 \sin \theta - 4 \cos \theta + 7}$ is
- a) $\frac{1}{12}$ b) $\frac{5}{12}$ c) $\frac{7}{12}$ d) $\frac{1}{6}$
16. If $\operatorname{cosec} \theta = \frac{p+q}{p-q}$, then $\cot(\pi/4 + \theta/2) =$
- a) $\sqrt{\frac{p}{q}}$ b) $\sqrt{\frac{q}{p}}$ c) \sqrt{pq} d) pq
17. Suppose $0 < t < \pi$ and $\sin t + \cos t = \frac{1}{5}$. Then, $\tan \frac{t}{2}$ is equal to
- a) 2 b) 3 c) $\frac{1}{3}$ d) 5
18. For what and only what values of α lying between 0 and π is the inequality $\sin \alpha \cos^3 \alpha > \sin^3 \alpha \cos \alpha$ valid?
- a) $\alpha \in (0, \pi/4)$ b) $\alpha \in (0, \pi/2)$ c) $\alpha \in (\pi/4, \pi/2)$ d) None of these
19. If $\alpha + \beta - \gamma = \pi$, then $\sin^2 \alpha + \sin^2 \beta - \sin^2 \gamma$ is equal to
- a) $2 \sin \alpha \sin \beta \cos \gamma$ b) $2 \cos \alpha \cos \beta \cos \gamma$ c) $2 \sin \alpha \sin \beta \sin \gamma$ d) None of these
20. If $\sec x \cos 5x + 1 = 0$, where $0 < x < 2\pi$, then x is equal to
- a) $\frac{\pi}{5}, \frac{\pi}{4}$ b) $\frac{\pi}{5}$ c) $\frac{\pi}{4}$ d) None of these

