

Topic :- TRIGONOMETRIC FUNCTIONS

1. The greatest and least value of $\sin x \cos x$ are respectively
 a) 1, -1 b) $\frac{1}{2}, -\frac{1}{2}$ c) $\frac{1}{4}, -\frac{1}{4}$ d) 2, -2
2. If $x = X \cos \theta - Y \sin \theta, y = X \sin \theta + Y \cos \theta$ and $x^2 + 4xy + y^2 = AX^2 + BY^2, 0 \leq \theta \leq \frac{\pi}{2}, n \in Z$, then
 a) $\theta = \frac{\pi}{6}, A = 3, B = 1$ b) $\theta = \frac{\pi}{2}, A = 3, B = 1$ c) $A = 3, B = -1, \theta = \frac{\pi}{4}$ d) $A = -3, B = 1, \theta = \frac{\pi}{4}$
3. The number of values of x in $[0, 2\pi]$ satisfying the equation $3 \cos 2x - 10 \cos x + 7 = 0$ is
 a) 1 b) 2 c) 3 d) 4
4. $\cos \alpha \sin(\beta - \gamma) + \cos \beta \sin(\gamma - \alpha) + \cos \gamma \sin(\alpha - \beta)$ is equal to
 a) 0 b) $\frac{1}{2}$ c) 1 d) $4 \cos \alpha \cos \beta \cos \gamma$
5. If $A + B = 45^\circ$, then $(\cot A - 1)(\cot B - 1)$ is equal to
 a) 1 b) $\frac{1}{2}$ c) -1 d) 2
6. The solution of the equation $[\sin x + \cos x]^{1 + \sin 2x} = 2, -\pi \leq x \leq \pi$ is
 a) $\frac{\pi}{2}$ b) π c) $\frac{\pi}{4}$ d) $\frac{3\pi}{4}$
7. If $\sin x + \sin^2 x = 1$, then the value of $\cos^{12} x + 3 \cos^{10} x + 3 \cos^8 x + \cos^6 x + 2 \cos^4 x + \cos^2 x - 2$, is equal to
 a) 0 b) 1 c) 2 d) $\sin^2 x$
8. $\sin^4 \frac{\pi}{8} + \sin^4 \frac{3\pi}{8} + \sin^4 \frac{5\pi}{8} + \sin^4 \frac{7\pi}{8}$ is equal to
 a) 1 b) $\frac{3}{2}$ c) 2 d) $\frac{1}{4}$
9. If $\sin(x + 3\alpha) = 3 \sin(\alpha - x)$, then
 a) $\tan x = \tan \alpha$ b) $\tan x = \tan^2 \alpha$ c) $\tan x = \tan^3 \alpha$ d) $\tan x = 3 \tan \alpha$
10. $\cos \alpha \sin(\beta - \gamma) + \cos \beta \sin(\gamma - \beta) + \cos \gamma \sin(\alpha - \beta) =$
 a) 0 b) $\frac{1}{2}$ c) 1 d) $4 \cos \alpha \cos \beta \cos \gamma$
11. If $\sin A + \cos A = m$ and $\sin^3 A + \cos^3 A = n$, then
 a) $m^3 - 3m + n = 0$ b) $n^3 - 3n + 2m = 0$ c) $m^3 - 3m + 2n = 0$ d) $m^3 + 3m + 2n = 0$
12. If $(\sec \theta - 1) = (\sqrt{2} - 1) \tan \theta$, then $\theta =$
 a) $n\pi + \frac{\pi}{8}, n \in Z$
 b) $2n\pi, 2n\pi + \frac{\pi}{4}, n \in Z$
 c) $2n\pi, n \in Z$
 d) None of these
13. The number of values of θ in the interval $[-\pi, \pi]$ satisfying the equation $\cos \theta + \sin 2\theta = 0$ is
 a) 1 b) 2 c) 3 d) 4

14. The general solution of $\tan\left(\frac{\pi}{2}\sin\theta\right) = \cot\left(\frac{\pi}{2}\cos\theta\right)$ is
- $\theta = 2r\pi + \frac{\pi}{2}, r \in Z$
 - $\theta = 2r\pi, r \in Z$
 - $\theta = 2r\pi + \frac{\pi}{2}$ and $\theta = 2r\pi, r \in Z$
 - None of these
15. The most general values of θ satisfying $\tan\theta + \tan\left(\frac{3\pi}{4} + \theta\right) = 2$ are given by
- $2n\pi \pm \frac{\pi}{3}, n \in Z$
 - $n\pi + \frac{\pi}{3}, n \in Z$
 - $2n\pi \pm \frac{\pi}{6}, n \in Z$
 - $n\pi \pm \frac{\pi}{6}, n \in Z$
16. If $(1 + \tan\theta)(1 + \tan\phi) = 2$, then $\theta + \phi =$
- 30°
 - 45°
 - 60°
 - 75°
17. If α and β satisfying $2\sec 2\alpha = \tan\beta + \cot\beta$, then $\alpha + \beta$ is equal to
- $\frac{\pi}{2}$
 - $\frac{\pi}{3}$
 - $\frac{\pi}{4}$
 - π
18. If $0 < \theta < 2\pi$, then the intervals of values of θ for which $2\sin^2\theta - 5\sin\theta + 2 > 0$, is
- $(0, \frac{\pi}{6}) \cup (\frac{5\pi}{6}, 2\pi)$
 - $(\frac{\pi}{8}, \frac{5\pi}{6})$
 - $(0, \frac{\pi}{8}) \cup (\frac{\pi}{6}, \frac{5\pi}{6})$
 - $(\frac{41\pi}{48}, \pi)$
19. If $\tan A - \tan B = x$ and $\cot B - \cot A = y$, then $\cot(A - B)$ is equal to
- $\frac{1}{x} + y$
 - $\frac{1}{xy}$
 - $\frac{1}{x} - \frac{1}{y}$
 - $\frac{1}{x} + \frac{1}{y}$
20. In a ΔABC , if a, c, b are in A.P., then the value of $\frac{a \cos B - b \cos A}{a - b}$, is
- 3
 - 2
 - 1
 - None of these

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