

Topic :-STATISTICS

141 (d)

Let x_1, x_2, \dots, x_n be n numbers. Then,

$$\bar{X} = \frac{1}{n} \sum_{i=1}^n x_i$$

If each number is divided by 3, then the new mean \bar{Y} is given by

$$\bar{Y} = \frac{1}{n} \sum_{i=1}^n \left(\frac{x_i}{3}\right) = \frac{1}{3} \left(\frac{1}{n} \sum_{i=1}^n x_i\right) = \frac{\bar{X}}{3}$$

142 (c)

Let $x_1, x_2, x_3, \dots, x_n$ be the variates corresponding to n sets of data, each having the same number of observations say k and x be their product. Then, $x = x_1, x_2, \dots, x_n$

$$\log x = \log x_1 + \log x_2 + \dots + \log x_n$$

$$\Rightarrow \frac{\sum \log x}{k} = \frac{\sum \log x_1}{k} + \frac{\sum \log x_2}{k} + \dots + \frac{\sum \log x_n}{k}$$

$$\Rightarrow \log G = \log G_1 + \log G_2 + \dots + \log G_n$$

$$\Rightarrow G = G_1 G_2 \dots G_n$$

143 (c)

Let the first natural number be x

According to the question,

$$x + x + 1 + x + 2 + x + 3 + x + 4 + x + 5 + x$$

$$+ 6 + x + 7 + x + 8 + x + 9 + x + 10 = 2761$$

$$\Rightarrow 11x + 55 = 2761$$

$$\Rightarrow x = \frac{2761 - 55}{11} = 246$$

$$\therefore \text{Middle number} = x + 5 = 246 + 5 = 251$$

144 (a)

We have, $4\bar{x} + 3\bar{y} + 7 = 0 \dots(i)$

And $3\bar{x} + 4\bar{y} + 8 = 0 \dots(ii)$

On solving Eqs.(i) and (ii), we get

$$\bar{x} = -\frac{4}{7} \text{ and } \bar{y} = -\frac{11}{7}$$

145 (b)

Let the n -numbers be x_1, x_2, \dots, x_n . Then,

$$\bar{X} = \frac{1}{n} \sum_{i=1}^n x_i$$

$$\Rightarrow \bar{X} = \frac{x_1 + x_2 + \dots + x_{n-1} + x_n}{n}$$

$$\Rightarrow \bar{X} = \frac{k + x_n}{n} \quad [\because x_1 + x_2 + \dots + x_{n-1} = k]$$

$$\Rightarrow x_n = n\bar{X} - k$$

146 (d)

$$\text{7th decile } D_7 = \frac{7n}{10} \dots \text{(i)}$$

$$\text{And 7th percentile, } P_{70} = \frac{7n}{100} \dots \text{(ii)}$$

From Eqs. (i) and (ii), we get

$$D_7 \neq P_{70}$$

149 (c)

Total of corrected observations

$$= 4500 - (91 + 13) + (19 + 31)$$

$$= 4446$$

$$\therefore \text{Mean} = \frac{4446}{100} = 44.46$$

150 (b)

$$\text{Given } b_{yx} = 0.8, b_{xy} = 0.2$$

$$\text{Then, } r = \sqrt{b_{xy}b_{yx}} = \sqrt{(0.8)(0.2)} = \sqrt{0.16}$$

$$\Rightarrow r = 0.4$$

152 (c)

Regression coefficient of y on x is given by $\frac{\text{cov}(x,y)}{\sigma_x^2}$

153 (a)

Let numbers of boys are x and numbers of girls are y .

$$\therefore 53(x + y) = 55y + 50x$$

$$\Rightarrow 3x = 2y$$

$$\Rightarrow x = \frac{2y}{3}$$

$$\therefore \text{total number of students} = x + y = \frac{2y}{3} + y = \frac{5}{3}y$$

Hence, required percentage

$$= \frac{y}{5y/3} \times 100\% = \frac{3}{5} \times 100\% = 60\%$$

154 (b)

Let n_1 and n_2 be the number of men and women in a group. According to the given condition,

$$\frac{n_1 \times 26 + n_2 \times 21}{n_1 + n_2} = 25$$

$$\Rightarrow 26n_1 + 21n_2 = 25n_1 + 25n_2$$

$$\Rightarrow n_1 = 4n_2 \Rightarrow \frac{n_1}{n_2} = \frac{4}{1}$$

$$\Rightarrow \frac{n_1}{n_2} = \frac{80}{20}$$

158 (d)

The intersecting point of two regression lines is on mean ie, (\bar{x}, \bar{y}) .

159 (b)

Let the regression coefficients be $b_{yx} = -0.33$

And $b_{xy} = -1.33$

$$\therefore r = -\sqrt{b_{yx} \times b_{xy}}$$

$$= -\sqrt{0.33 \times 1.33}$$

$$= -\sqrt{0.4389}$$

$$= -0.66$$

160 (c)

$$\text{Cov}(x, y) = \frac{\Sigma xy}{n} - \frac{\Sigma x}{n} \cdot \frac{\Sigma y}{n} = \frac{1}{10}(850) - \left(\frac{30}{10}\right)\left(\frac{400}{10}\right)$$

$$= 85 - 120 = -35$$

$$\text{And var}(x) = \sigma_x^2 = \frac{1}{n}\Sigma x^2 - \left(\frac{\Sigma x}{n}\right)^2$$

$$= \frac{196}{10} - \left(\frac{30}{10}\right)^2 = 10.6$$

$$\therefore b_{yx} = \frac{\text{cov}(x, y)}{\text{var}(x)} = \frac{-35}{10.6} = -3.3$$

ANSWER-KEY

Q.	1	2	3	4	5	6	7	8	9	10
A.	D	C	C	A	B	D	D	A	C	B
Q.	11	12	13	14	15	16	17	18	19	20
A.	C	C	A	B	C	A	A	D	B	C