

Topic :-STATISTICS

122 (c)

$$r_{xy} = \frac{\text{cov}(x,y)}{\sqrt{\text{var}(x)\text{var}(y)}} \\ = \frac{10.2}{\sqrt{(8.25)(33.96)}} = 0.61$$

124 (b)

Let us assume that line of regression y on x is $3x + 12y = 19$ and x on y is $3y + 9x = 46$.

$$\therefore b_{yx} = -\frac{3}{12} \text{ and } b_{xy} = -\frac{3}{9} = -\frac{1}{3}$$

$$\therefore r_{xy} = -\sqrt{b_{yx} \times b_{xy}} = -\sqrt{\left(\frac{3}{12}\right) \times \left(\frac{1}{3}\right)}$$

$$= -\sqrt{\frac{1}{12}} = -\sqrt{0.083}$$

$$= -0.289$$

125 (c)

$$\text{Cov}(x,y) = \frac{1}{n}\sum xy - \bar{x}\bar{y} \\ = \frac{1}{2}(110) - \left(\frac{15}{5}\right)\left(\frac{36}{5}\right) = \frac{2}{5}$$

127 (d)

Let $x_1, x_2, x_3, \dots, x_n$ be n observation

$$\therefore \bar{x} = \frac{\sum x_i}{n} \dots(i)$$

$$\text{New mean} = \frac{\sum x_i + x_{n+1}}{n+1}$$

$$\text{According to the question } \bar{x} = \frac{\sum x_i + x_{n+1}}{n+1}$$

$$\Rightarrow (n+1)\bar{x} = n\bar{x} + x_{n+1}$$

$$\Rightarrow x_{n+1} = \bar{x}$$

130 (c)

Let $x_1, x_2, x_3, \dots, x_n$ be n observations. Then,

$$\bar{x} = \frac{1}{n} \sum_{i=1}^n x_i$$

$$\therefore \text{New mean, } \bar{X} = \frac{1}{n} \sum_{i=1}^n \left(\frac{x_i}{\alpha} + 10 \right)$$

$$= \frac{1}{\alpha} \left(\frac{1}{n} \sum_{i=1}^n x_i \right) + \frac{1}{n} \cdot (10n)$$

$$= \frac{1}{\alpha} \bar{x} + 10 = \frac{\bar{x} + 10\alpha}{\alpha}$$

131 (b)

Since, there are 19 observations. So, the middle term is 10th

After including 8 and 32, i.e., 8 will come before 30 and 32 will come after 30

Here, new median will remain 30

132 (b)

We have,

$$\sigma^2 = \frac{1}{n} \sum_{i=1}^n x_i^2 - \left(\frac{1}{n} \sum_{i=1}^n x_i \right)^2$$

$$\Rightarrow \sigma^2 = \frac{1}{n} (1^2 + 2^2 + \dots + n^2) - \left(\frac{1}{n} (1 + 2 + \dots + n) \right)^2$$

$$\Rightarrow \sigma^2 = \frac{1}{n} \times \frac{n(n+1)(2n+1)}{6} - \left(\frac{n+1}{2} \right)^2 = \frac{n^2 - 1}{12}$$

133 (c)

Class f_i y_i $D_i = y_i - A$

$A = 25$ $f_i d_i f_i d_i^2$

0-10	1	5	-20	-20	400
10-20	3	15	-10	-30	300
20-30	4	25	0	0	0
30-40	2	35	10	20	200
Total	10			-30	900

$$\therefore \sigma^2 = \frac{\sum f_i d_i^2}{\sum f_i} - \left(\frac{\sum f_i d_i}{\sum f_i} \right)^2$$

$$= \frac{900}{10} - \left(\frac{-30}{10} \right)^2 = 90 - 9$$

$$\Rightarrow \sigma^2 = 81$$

$$\Rightarrow \sigma = 9$$

134 (a)

Arranging the given values in ascending order of magnitude

$$x - \frac{7}{2}, x - 3, x - \frac{5}{2}, x - 2, x + \frac{1}{2}, x + 4, x + 5$$

There are 8 observations in the series, therefore

$$\text{median} = \frac{\text{Value of 4th term} + \text{Value of 5th term}}{2}$$

$$= \frac{x - 2 + x - \frac{1}{2}}{2} = x - \frac{5}{4}$$

136 (d)

The required AM is given by

$$\text{AM} = \frac{1}{n} \sum_{i=1}^n (i+1)x_i$$

$$\Rightarrow \text{AM} = \frac{1}{n} \sum_{i=1}^n (i+1)i$$

$$\Rightarrow \text{AM} = \frac{1}{n} \left\{ \sum_{i=1}^n (i^2 + i) \right\}$$

$$\Rightarrow \text{AM} = \frac{1}{n} \left\{ \sum_{i=1}^n i^2 + \sum_{i=1}^n i \right\}$$

$$\Rightarrow \text{AM} = \frac{1}{n} \left\{ \frac{n(n+1)(2n+1)}{6} + \frac{n(n+1)}{2} \right\}$$

$$\Rightarrow \text{AM} = \frac{(n+1)(2n+1)}{6} + \frac{n+1}{2}$$

$$\Rightarrow \text{AM} = \frac{(n+1)(5n+4)}{6}$$

PEE

ANSWER-KEY

Q.	1	2	3	4	5	6	7	8	9	10
A.	A	C	C	B	C	C	D	C	D	C
Q.	11	12	13	14	15	16	17	18	19	20
A.	B	B	C	A	C	D	A	B	B	C