

Topic :-STATISTICS

61 **(d)**
 Median of new set remains the same as that of the original set.

62 **(a)**

$$\bar{x} = \frac{8 + 12 + 13 + 15 + 22}{5} = \frac{70}{5} = 14$$

$$\sigma = \sqrt{\frac{(8 - 14)^2 + (12 - 14)^2 + (13 - 14)^2 + (15 - 14)^2 + (22 - 14)^2}{5}}$$

$$= \sqrt{\frac{36 + 4 + 1 + 1 + 64}{5}}$$

$$= \sqrt{212} = 4.604$$

63 **(b)**
 The formula for combined mean is

$$\bar{X} = \frac{n_1\bar{X}_1 + n_2\bar{X}_2}{n_1 + n_2}$$

We are given $\bar{X} = 25$, $\bar{X}_1 = 26$, $\bar{X}_2 = 21$. Let $n_1 + n_2 = 100$
 and n_1 denotes men and n_2 denotes women

$$n_2 = 100 - n_1$$

$$\therefore 25 = \frac{26n_1 + 21(100 - n_1)}{100} \Rightarrow n_1 = 80$$

$$\text{So, } n_2 = 20$$

Hence, the percentage of men and women is 80 and 20 respectively

64 **(b)**
 Taking X as the product of variates X_1, X_2, \dots, X_r corresponding to r sets of observations i.e.
 $X = X_1 X_2 \dots X_r$, we have

$$\log X = \log X_1 + \log X_2 + \dots + \log X_r$$

$$\Rightarrow \sum \log X = \sum \log X_1 + \sum \log X_2 + \dots + \sum \log X_r$$

$$\Rightarrow \frac{1}{n} \sum \log X = \frac{1}{n} \sum \log X_1 + \frac{1}{n} \sum \log X_2 + \dots + \frac{1}{n} \sum \log X_r$$

$$\Rightarrow \log G = \log G_1 + \log G_2 + \dots + \log G_r$$

$$\Rightarrow G = G_1 G_2 \dots G_r$$

68

(a)

For a moderately skewed distribution, we have

$$\text{Mode} = 3 \text{ Median} - 2 \text{ Mean}$$

$$\Rightarrow \text{Mode} = 3(6) - 2(5) = 8$$

69

(d)

Let n_1 and n_2 be the number of observations in two groups having means \bar{X}_1 and \bar{X}_2 respectively

$$\text{Then, } \bar{X} = \frac{n_1 \bar{X}_1 + n_2 \bar{X}_2}{n_1 + n_2}$$

$$\text{Now, } \bar{X} - \bar{X}_1 = \frac{n_1 \bar{X}_1 + n_2 \bar{X}_2}{n_1 + n_2} - \bar{X}_1$$

$$= n_2 \frac{(\bar{X}_2 - \bar{X}_1)}{n_1 + n_2} > 0 \quad (\because \bar{X}_2 > \bar{X}_1)$$

$$\Rightarrow \bar{X} > \bar{X}_1 \quad \dots(i)$$

$$\text{And } \bar{X} - \bar{X}_2 = \frac{n_1(\bar{X}_1 - \bar{X}_2)}{n_1 + n_2} < 0 \quad \because \bar{X}_2 > \bar{X}_1$$

$$\Rightarrow \bar{X} < \bar{X}_2 \quad \dots(ii)$$

From relations (i) and (ii), we get

$$\bar{X}_1 < \bar{X} < \bar{X}_2$$

71

(b)

$$\text{Given lines are } 3\bar{x} - 2\bar{y} + 1 = 0 \quad \dots(i)$$

$$\text{And } 2\bar{x} - \bar{y} - 2 = 0 \quad \dots(ii)$$

On solving Eqs. (i) and (ii), we get $\bar{x} = 5, \bar{y} = 8$

72

(c)

It is true that mode can be computed from histogram and median is not independent of change of scale.

But variance is independent of change of origin and not of scale.

77

(c)

$$r_{xy} = \frac{\sum (x - \bar{x})(y - \bar{y})}{\sqrt{\sum (x - \bar{x})^2 \sum (y - \bar{y})^2}}$$

$$= \frac{20}{\sqrt{36 \times 25}} = \frac{2}{3} = 0.66$$

78

(c)

Correlation coefficient,

$$r = \frac{n \sum xy - \sum x \sum y}{\sqrt{\{n \sum x^2 - (\sum x)^2\} \{n \sum y^2 - (\sum y)^2\}}}$$

$$= \frac{10(220) - 40 \times 50}{\sqrt{10(200) - (40)^2} \sqrt{10(262) - (50)^2}}$$

$$= \frac{200}{20 \times 10.954} = \frac{200}{219.08} = 0.91$$

79

(a)

Let us assume that line of regression y on x is $4y = 3$ and x on y is $3x + y = 15$.

\therefore put $y = 3$ in $3x + y = 15$

$$\Rightarrow 3x = 15 - 3$$
$$x = 4$$

ANSWER-KEY										
Q.	1	2	3	4	5	6	7	8	9	10
A.	D	A	B	B	D	C	A	A	D	B
Q.	11	12	13	14	15	16	17	18	19	20
A.	B	C	C	B	A	B	C	C	A	C

PE