

Topic :-SETS

142 (d)

Clearly, R is neither reflexive, nor symmetric and not transitive

143 (d)

Clearly, given relation is an equivalence relation

145 (c)

Each subset will contain 3 and any number of elements from the remaining 3 elements 1, 2 and 4

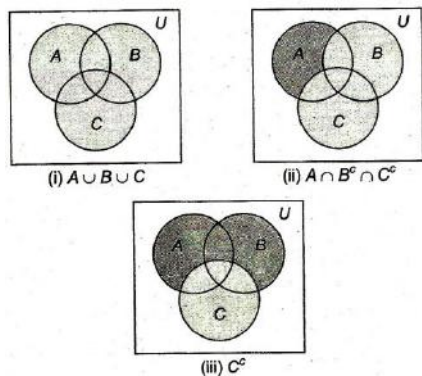
So, required number of elements = $2^2 = 8$

146 (a)

Since $(1,1), (2,2), (3,3) \in R$. Therefore, R is reflexive. We observe that $(1,2) \in R$ but $(2,1) \notin R$, therefore R is not symmetric.

It can be easily seen that R is transitive

147 (b)



From figures (i), (ii) and (iii), we get

$$(A \cup B \cup C) \cap (A \cap B^c \cap C^c) \cap C^c = (B^c \cap C^c)$$

148 (d)

A relation on set A is a subset of $A \times A$

Let $A = \{a_1, a_2, \dots, a_n\}$. Then, a reflexive relation on A must contain at least n elements $(a_1, a_1), (a_2, a_2), \dots, (a_n, a_n)$

\therefore Number of reflexive relations on A is 2^{n^2-n}

Clearly, $n^2 - n = n, n^2 - n = n - 1, n^2 - n = n^2 - 1$ have solutions in N but $n^2 - n = n + 1$ is not solvable in N .

So, 2^{n+1} cannot be the number of reflexive relations on A

149 (a)

We have,

$$A \Delta B = (A \cup B) - (A \cap B)$$

$$\Rightarrow n(A \Delta B) = n(A) + n(B) - 2n(A \cap B)$$

So, $n(A \Delta B)$ is greatest when $n(A \cap B)$ is least

It is given that $A \cap B \neq \phi$. So, least number of elements in $A \cap B$ can be one

$$\therefore \text{Greatest possible value of } n(A \Delta B) \text{ is } 7 + 6 - 2 \times 1 = 11$$

150 (d)

Let $R = \{(x,y):y = ax + b\}$. Then,

$$(-2, -7), (-1, -4) \in R$$

$$\Rightarrow -7 = -2a + b \text{ and } -4 = -a + b$$

$$\Rightarrow a = 3, b = -1$$

$$\therefore y = 3x - 1$$

$$\text{Hence, } R = \{(x,y):y = 3x - 1, -2 \leq x < 3, x \in Z\}$$

151 (a)

Let U be the set of all students in the school. Let C, H and B denote the sets of students who played cricket, hockey and basketball respectively. Then,

$$n(U) = 800, n(C) = 224, n(H) = 240, n(B) = 336$$

$$n(H \cap B) = 64, n(B \cap C) = 80, n(H \cap C) = 40$$

$$\text{and, } n(H \cap B \cap C) = 24$$

\therefore Required number

$$= n(C' \cap H' \cap B')$$

$$= n(C \cup H \cup B)'$$

$$= n(U) - n(C \cup H \cup B)$$

$$= n(U) - \{n(C) + n(H) + n(B) - n(C \cap H) - n(H \cap B) - n(B \cap C) + n(C \cap H \cap B)\}$$

$$= 800 - \{224 + 240 + 336 + 336 - 64 - 80 - 40 + 24\}$$

$$= 800 - 640 = 160$$

152 (c)

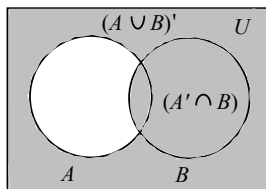
According to question,

$$2^m - 2^n = 48$$

This is possible only if $m = 6$ and $n = 4$.

153 (a)

From Venn-Euler's Diagram it is clear that



$$(A \cup B)' \cup (A' \cap B) = A'$$

154 (b)

For any $a, b \in R$

$$a \neq b \Rightarrow b \neq a \Rightarrow R \text{ is symmetric}$$

Clearly, $2 \neq -3$ and $-3 \neq 2$, but $2 = 2$. So, R is not transitive.

Clearly, R is not reflexive

155 (a)

We have,

$$A \Delta B = (A \cup B) - (A \cap B)$$

$$\Rightarrow n(A \Delta B) = n(A) + n(B) - 2n(A \cap B)$$

So, $n(A \Delta B)$ is greatest when $n(A \cap B)$ is least

It is given that $A \cap B \neq \phi$. So, least number of elements in $A \cap B$ can be one

$$\therefore \text{Greatest possible value of } n(A \Delta B) \text{ is } 7 + 6 - 2 \times 1 = 11$$

156 (c)

Since $x \not\prec x$, therefore R is not reflexive

Also, $x < y$ does not imply that $y < x$

So R is not symmetric

Let $x R y$ and $y R z$. Then, $x < y$ and $y < z \Rightarrow x < z$ i.e. $x R z$

Hence, R is transitive

157 (b)

Number of elements common to each set is $99 \times 99 = 99^2$.

158 (b)

Given, $A \cap X = B \cap X = \phi$

$\Rightarrow A$ and X, B and X are disjoint sets.

Also, $A \cup X = B \cup X \Rightarrow A = B$

160 (c)

Clearly, R is reflexive and symmetric but it is not transitive

ANSWER-KEY

Q.	1	2	3	4	5	6	7	8	9	10
A.	B	D	D	A	C	A	B	D	A	D
Q.	11	12	13	14	15	16	17	18	19	20
A.	A	C	A	B	A	C	B	B	A	C