

Topic :-SETS

21 (c)

$$\begin{aligned}A \cap B &= \{x : x \text{ a multiple of } 3\} \text{ and } \{x : x \text{ is a multiple of } 5\} \\ &= \{x : x \text{ is a multiple of } 15\} \\ &= \{15, 30, 45, \dots\}\end{aligned}$$

22 (b)

We have,

$$n(A \times B) = 45$$

$$\Rightarrow n(A) \times n(B) = 45$$

$\Rightarrow n(A)$ and $n(B)$ are factors of 45 such that their product is 45

Hence, $n(A)$ cannot be 17

24 (a)

For any $x \in R$, we have

$$x - x + \sqrt{2} = \sqrt{2} \text{ an irrational number}$$

$$\Rightarrow x R x \text{ for all } x$$

So, R is reflexive

R is not symmetric, because $\sqrt{2} R 1$ but $1 \not R \sqrt{2}$

R is not transitive also because $\sqrt{2} R 1$ and $1 R 2\sqrt{2}$ but $\sqrt{2} \not R 2\sqrt{2}$

25 (b)

We have,

$$n(H) - n(H \cap E) = 22, n(E) - n(H \cap E) = 12, n(H \cup E) = 45$$

$$\therefore n(H \cup E) = n(H) + n(E) - n(H \cap E)$$

$$\Rightarrow 45 = 22 + 12 + n(H \cap E)$$

$$\Rightarrow n(H \cap E) = 11$$

26 (c)

We have, $A \subset B$ and $B \subset C$

$$\therefore A \cup B = B \text{ and } B \cap C = B$$

$$\Rightarrow A \cup B = B \cap C$$

27 (c)

$$\text{Let } A = \left\{ x \in R : \frac{2x-1}{x^3+4x^2+3x} \right\}$$

$$\text{Now, } x^3+4x^2+3x = x(x^2+4x+3)$$

$$= x(x+3)(x+1)$$

$$\therefore A = R - \{0, -1, -3\}$$

29 **(d)**

Clearly, $y^2 = x$ and $y = |x|$ intersect at $(0,0), (1,1)$ and $(-1, -1)$. Hence, option (d) is correct

31 **(d)**

Let M, P and C be the sets of students taking examinations in Mathematics, Physics and Chemistry respectively.

We have,

$$n(M \cup P \cup C) = 50, n(M) = 37, n(P) = 24, n(C) = 43$$

$$n(M \cap P) < 19, n(M \cap C) \leq 29, n(P \cap C) \leq 20$$

Now,

$$\begin{aligned} n(M \cup P \cup C) &= n(M) + n(P) + n(C) - n(M \cap P) \\ &\quad - n(M \cap C) - n(P \cap C) + n(M \cap P \cap C) \\ \Rightarrow 50 &= 37 + 24 + 43 - \{n(M \cap P) + n(M \cap C) + n(P \cap C)\} \\ &\quad + n(M \cap P \cap C) \\ \Rightarrow n(M \cap P \cap C) &= n(M \cap P) + n(M \cap C) + n(P \cap C) - 54 \\ \Rightarrow n(M \cap P) + n(M \cap C) + n(P \cap C) \\ &= n(M \cap P \cap C) + 54 \quad \dots(i) \end{aligned}$$

Now,

$$\begin{aligned} n(M \cap P) \leq 19, n(M \cap C) \leq 29, n(P \cap C) \leq 20 \\ \Rightarrow n(M \cap P) + n(M \cap C) + n(P \cap C) &\leq 19 + 29 + 20 \quad [\text{Using (i)}] \\ \Rightarrow n(M \cap P \cap C) + 54 &\leq 68 \\ \Rightarrow n(M \cap P \cap C) &\leq 14 \end{aligned}$$

33 **(a)**

Given, $n(N) = 12, n(P) = 16, n(H) = 18,$

$$n(N \cup P \cup H) = 30$$

And $n(N \cap P \cap H) = 0$

$$\begin{aligned} \text{Now, } n(N \cup P \cup H) &= n(N) + n(P) + n(H) \\ &\quad - n(N \cap P) - n(P \cap H) - n(H \cap N) \\ &\quad + n(N \cap P \cap H) \\ \Rightarrow n(N \cap P) + n(P \cap H) + n(H \cap N) &= (12 + 16 + 18) - 30 \\ &= 46 - 30 = 16 \end{aligned}$$

35 **(b)**

The void relation R on A is not reflexive as $(a,a) \notin R$ for any $a \in A$. The void relation is symmetric and transitive

36 **(c)**

Given, A 's are 30 sets with five elements each, so

$$\sum_{i=1}^{30} n(A_i) = 5 \times 30 = 150 \quad \dots(i)$$

If the m distinct elements in S and each elements of S belongs to exactly 10 of the A_i 's, then

$$\sum_{i=1}^{30} n(A_i) = 10m \quad \dots(ii)$$

From Eqs. (i) and (ii), $m = 15$

Similarly, $\sum_{j=1}^n n(B_j) = 3n$ and $\sum_{j=1}^n n(B_j) = 9m$

$$\therefore 3n = 9m$$

$$\Rightarrow n = \frac{9m}{3} = 3 \times 15 = 45$$

38 (b)

$A \cup B$ will contain minimum number of elements if $A \subset B$ and in that case, we have

$$n(A \cup B) = n(B) = 6$$

40 (c)

It is given that $A_1 \subset A_2 \subset A_3 \subset \dots \subset A_{100}$

$$\therefore \bigcup_{i=3}^{100} A_i = A \Rightarrow A_3 = A \Rightarrow n(A) = n(A_3) = 3 + 2 = 5$$

ANSWER-KEY										
Q.	1	2	3	4	5	6	7	8	9	10
A.	C	B	D	A	B	C	C	A	D	C
Q.	11	12	13	14	15	16	17	18	19	20
A.	D	C	A	B	B	C	B	B	B	C