

Topic :-RELATIONS AND FUNCTIONS

- The function $f:R \rightarrow R$ given by $f(x) = x^3 - 1$ is
 - A one-one function
 - An onto function
 - A bijection
 - Neither one-one nor onto
- Let $[x]$ denote the greatest integer $\leq x$. If $f(x) = [x]$ and $g(x) = |x|$, then the value of $f\left(g\left(\frac{8}{5}\right)\right) - g\left(f\left(-\frac{8}{5}\right)\right)$ is
 - 2
 - 2
 - 1
 - 1
- The domain of the function $f(x) = \frac{\cos^{-1}x}{[x]}$ is
 - $[-1, 0) \cup \{1\}$
 - $[-1, 1]$
 - $[-1, 1)$
 - None of these
- The set of values of x for which of the function $f(x) = \frac{1}{x} + 2^{\sin^{-1}x} + \frac{1}{\sqrt{x-2}}$ exists is
 - R
 - $R - \{0\}$
 - ϕ
 - None of these
- If $f(x)$ satisfies the relation $2f(x) + f(1-x) = x^2$ for all real x , then $f(x)$ is
 - $\frac{x^2 + 2x - 1}{6}$
 - $\frac{x^2 + 2x - 1}{3}$
 - $\frac{x^2 + 4x - 1}{3}$
 - $\frac{x^2 - 3x + 1}{6}$
- If the function $f(x)$ is defined by $f(x) = a + bx$ and $f^r = fff \dots$ (repeated r times), then $f^r(x)$ is equal to
 - $a + b^r x$
 - $ar + b^r x$
 - $ar + bx^r$
 - $a\left(\frac{b^r - 1}{b - 1}\right) + b^r x$
- If $f(x) = \frac{x-1}{x+1}$, then $f(2x)$ is
 - $\frac{f(x)+1}{f(x)+3}$
 - $\frac{3f(x)+1}{f(x)+3}$
 - $\frac{f(x)+3}{f(x)+1}$
 - $\frac{f(x)+3}{3f(x)+1}$
- If $f(x)$ is an odd periodic function with period 2, then $f(4)$ equals
 - 0
 - 2
 - 4
 - 4

9. The domain of definition of

$$f(x) = \sqrt{\log_{0.4} \left(\frac{x-1}{x+5} \right)} \times \frac{1}{x^2 - 36}, \text{ is}$$

- a) $(-\infty, 0) - \{-6\}$ b) $(0, \infty) - \{1, 6\}$ c) $(1, \infty) - \{6\}$ d) $[1, \infty) - \{6\}$

10. The domain of the function $f(x) = \log_2(\log_3(\log_4 x))$ is

- a) $(-\infty, 4)$ b) $(4, \infty)$ c) $(0, 4)$ d) $(1, \infty)$

11. Let $f(x) = |x - 2| + |x - 3| + |x - 4|$ and $g(x) = x + 1$. Then,

- a) $g(x)$ is an even function
b) $g(x)$ is an odd function
c) $g(x)$ is neither even nor odd
d) $g(x)$ is periodic

12. If a function $f : [2, \infty) \rightarrow B$ defined by $f(x) = x^2 - 4x + 5$ is a bijection, then $B =$

- a) R b) $[1, \infty)$ c) $[4, \infty)$ d) $[5, \infty)$

13. R is relation on N given by $R = \{(x, y) : 4x + 3y = 20\}$. Which of the following belongs to R ?

- a) $(-4, 12)$ b) $(5, 0)$ c) $(3, 4)$ d) $(2, 4)$

14. If $f: R \rightarrow R$ be a mapping defined by $f(x) = x^3 + 5$, then $f^{-1}(x)$ is equal to

- a) $(x + 5)^{1/3}$ b) $(x - 5)^{1/3}$ c) $(5 - x)^{1/3}$ d) $5 - x$

15. Let $f(x) = x$ and $g(x) = |x|$ for all $x \in R$. Then, the function $\phi(x)$ satisfying $[\phi(x) - f(x)]^2 + [\phi(x) - g(x)]^2 = 0$

- a) $\phi(x) = x, x \in [0, \infty)$
b) $\phi(x) = x, x \in R$
c) $\phi(x) = -x, x \in (-\infty, 0]$
d) $\phi(x) = x + |x|, x \in R$

16. In a function $f(x)$ is defined for $x \in [0, 1]$, then the function $f(2x + 3)$ is defined for

- a) $x \in [0, 1]$ b) $x \in [-3/2, -1]$ c) $x \in R$ d) $x \in [-3/2, 1]$

17. If $f(x) = x^2 - 2|x|$ and

$$g(x) = \begin{cases} \text{Min}\{f(t) : -2 \leq t \leq x\}, & -2 \leq x < 0 \\ \text{Max}\{f(t) : 0 \leq t \leq x\}, & 0 \leq x \leq 3 \end{cases}, \text{ then } g(x) \text{ equals}$$

$$\text{a) } \begin{cases} x^2 - 2x, & -2 \leq x \leq -1 \\ -1, & -1 \leq x < 0 \\ 0, & 0 \leq x < 2 \\ x^2 + 2x, & 2 \leq x \leq 3 \end{cases}$$

$$\text{b) } \begin{cases} x^2 + 2x, & -2 \leq x \leq -1 \\ -1, & -1 \leq x < 0 \\ 0, & 0 \leq x < 1 \\ x^2 - 2x, & 1 \leq x \leq 3 \end{cases}$$

$$c) \begin{cases} x^2 + 2x, & -2 \leq x \leq 0 \\ x^2 - 2x, & 0 \leq x \leq 3 \end{cases}$$

$$d) \begin{cases} x^2 + 2x, & -2 \leq x \leq 0 \\ 0, & 0 \leq x < 2 \\ x^2 - 2x, & 2 \leq x \leq 3 \end{cases}$$

18. Let R be the set of real numbers and the mapping $f:R \rightarrow R$ and $g:R \rightarrow R$ be defined by $f(x) = 5 - x^2$ and $g(x) = 3x - 4$, then the value of $(f \circ g)(-1)$ is

- a) -44 b) -54 c) -32 d) -64

19. $f:R \rightarrow R$ is defined by $f(x) = \frac{e^{x^2} - e^{-x^2}}{e^{x^2} + e^{-x^2}}$, is

- a) One-one but not onto
 b) Many-one but onto
 c) One-one and onto
 d) Neither one-one nor onto

20. Let $f:N \rightarrow N$ defined by $f(x) = x^2 + x + 1$, $x \in N$, then f is

- a) One-one onto b) Many-one onto c) One-one but not onto d) None of these

