

## Topic :-RELATIONS AND FUNCTIONS

- Let  $A = \{x : -1 \leq x \leq 1\}$  and  $f : A \rightarrow A$  such that  $f(x) = x|x|$ , then  $f$  is
  - A bijection
  - Injective but not surjective
  - Surjective but not injective
  - Neither injective nor surjective
- The domain of the function  $\sin^{-1}\left(\log_2 \frac{x^2}{2}\right)$  is
  - $[-1, 2] - \{0\}$
  - $[-2, 2] - (-1, 1)$
  - $[-2, 2] - \{0\}$
  - $[1, 2]$
- If  $f(x) = ax + b$  and  $g(x) = cx + d$ , then  $f\{g(x)\} = g\{f(x)\}$  is equivalent to
  - $f(a) = f(c)$
  - $f(b) = g(b)$
  - $f(d) = g(b)$
  - $f(c) = g(a)$
- The period of the function  $f(x) = \sin^4 3x + \cos^4 3x$  is
  - $\pi/2$
  - $\pi/3$
  - $\pi/6$
  - None of these
- Given  $f(x) = \log_{10} \left(\frac{1+x}{1-x}\right)$  and  $g(x) = \frac{3x+x^3}{1+3x^2}$ , then  $f \circ g(x)$  equals
  - $-f(x)$
  - $3f(x)$
  - $[f(x)]^3$
  - None of these
- Which of the following functions is not an injective map(s)?
  - $f(x) = |x + 1|, x \in [-1, \infty)$
  - $g(x) = x + \frac{1}{x}, x \in (0, \infty)$
  - $h(x) = x^2 + 4x - 5, x \in (0, \infty)$
  - $h(x) = e^{-x}, x \in [0, \infty)$
- If  $f: R \rightarrow R$  and  $g: R \rightarrow R$  are defined by  $f(x) = x - [x]$  and  $g(x) = [x]$  for  $x \in R$ , where  $[x]$  is the greatest integer not exceeding  $x$ , then for every  $x \in R$ ,  $f(g(x))$  is equal to
  - $x$
  - $0$
  - $f(x)$
  - $g(x)$
- The domain of definition of  $f(x) = \sqrt{\frac{\log_{0.3}|x-2|}{|x|}}$ , is
  - $[1, 2) \cup (2, 3]$
  - $[1, 3]$
  - $R - (1, 3]$
  - None of these
- $f: R \rightarrow R$  given by  $f(x) = 5 - 3\sin x$ , is
  - One-one
  - Onto
  - One-one and onto
  - None of these

10. If  $f(x + 2y, x - 2y) = xy$ , then  $f(x, y)$  equals  
 a)  $\frac{x^2 - y^2}{8}$                       b)  $\frac{x^2 - y^2}{4}$                       c)  $\frac{x^2 + y^2}{4}$                       d)  $\frac{x^2 - y^2}{2}$
11. If  $f: R \rightarrow R$  is defined as  $f(x) = (1 - x)^{1/3}$ , then  $f^{-1}(x)$  is  
 a)  $(1 - x)^{-1/3}$                       b)  $(1 - x)^3$                       c)  $1 - x^3$                       d)  $1 - x^{1/3}$
12. If  $f(x + 2y, x, x - 2y) = xy$ , then  $f(x, y)$  equals  
 a)  $\frac{x^2 - y^2}{8}$                       b)  $\frac{x^2 - y^2}{4}$                       c)  $\frac{x^2 + y^2}{4}$                       d)  $\frac{x^2 - y^2}{2}$
13. Let  $f: [4, \infty[ \rightarrow [4, \infty[$  be defined by  $f(x) = 5^{x(x-4)}$  then  $f^{-1}(x)$   
 a)  $2 - \sqrt{4 + \log_5 x}$                       b)  $2 + \sqrt{4 + \log_5 x}$                       c)  $\left(\frac{1}{5}\right)^{x(x-4)}$                       d) Not defined
14. If  $f: [2, 3] \rightarrow R$  is defined by  $f(x) = x^3 + 3x - 2$ , then the range  $f(x)$  is contained in the interval  
 a)  $[1, 12]$                       b)  $[12, 34]$                       c)  $[35, 50]$                       d)  $[-12, 12]$
15. The period of  $\sin^2 \theta$ , is  
 a)  $\pi^2$                       b)  $\pi$                       c)  $2\pi$                       d)  $\pi/2$
16. If  $n \in N$ , and the period of  $\frac{\cos nx}{\sin(\frac{x}{n})}$  is  $4\pi$ , then  $n$  is equal to  
 a) 4                      b) 3                      c) 2                      d) 1
17. For real  $x$ , let  $f(x) = x^3 + 5x + 1$ , then  
 a)  $f$  is one-one but not onto  $R$                       b)  $f$  is onto  $R$  but not one-one  
 c)  $f$  is one-one and onto  $R$                       d)  $f$  is neither one-one nor onto  $R$
18. The range of the function  $f(x) = \frac{1}{2 - \cos 3x}$  is  
 a)  $[-1/3, 0]$                       b)  $R$                       c)  $[1/3, 1]$                       d) None of these
19. Let  $A = \{2, 3, 4, 5, \dots, 16, 17, 18\}$ . Let be the equivalence relation on  $A \times A$ , cartesian product of  $A$  and  $A$ , defined by  $(a, b) \approx (c, d)$  if  $ad = bc$ , then the number of ordered pairs of the equivalence class of  $(3, 2)$  is  
 a) 4                      b) 5                      c) 6                      d) 7
20. Let  $n$  be the natural number. Then, the range of the function  $f(n) = 8 - n_{p_{n-4}}$ ,  $4 \leq n \leq 6$ , is  
 a)  $\{1, 2, 3, 4\}$                       b)  $\{1, 2, 3, 4, 5, 6\}$                       c)  $\{1, 2, 3\}$                       d)  $\{1, 2, 3, 4, 5\}$