

Topic :-PROBABILITY

1 (c)

Given, $f(x) = \frac{x}{2}$ $[0 \leq x \leq 2]$

$$\therefore P(X > 1.5) = \int_{1.5}^2 \frac{x}{2} dx = \left[\frac{x^2}{4} \right]_{1.5}^2$$

$$= 0.4375$$

$$\text{and } P(X > 1) = \int_1^2 \frac{x}{2} dx = \left[\frac{x^2}{4} \right]_1^2 = 0.75$$

$$\therefore P\left(\frac{X > 1.5}{X > 1}\right) = \frac{P(X > 1.5)}{P(X > 1)}$$

$$= \frac{0.4375}{0.75} = \frac{7}{12}$$

2 (a)

$$\text{Required probability} = 1 - \left(1 - \frac{2}{3}\right)\left(1 - \frac{3}{4}\right) = \frac{11}{12}$$

3 (a)

Given, $P(A \cup B) = 0.6$, $P(A \cap B) = 0.2$

Probability of exactly one of the event occurs is

$$P(\bar{A} \cap B) + P(A \cap \bar{B})$$

$$= P(B) - P(A \cap B) + P(A) - P(A \cap B)$$

$$= P(A \cup B) + P(A \cap B) - 2P(A \cap B)$$

$$[\because P(A \cup B) = P(A) + P(B) - P(A \cap B)]$$

$$= P(A \cup B) - P(A \cap B)$$

$$= 0.6 - 0.2 = 0.4$$

4 (c)

Probability of each case = $\frac{9}{15} = \frac{3}{5}$

Required probability (with replacement) = $\left(\frac{3}{5}\right)^7$

5 (b)

The total number of ways = $6^3 = 216$

If the second number is $i (i > 1)$, then the total number of favourable ways

$$= \sum_{i=1}^5 (i-1)(6-i) = 20$$

$$\therefore \text{Required probability} = \frac{20}{216} = \frac{5}{54}$$

6 (b)

$$\frac{P(X=K)}{P(X=k-1)} = \frac{{}^n C_k p^k q^{n-k}}{{}^n C_{k-1} p^{k-1} q^{n-k+1}}$$

$$= \left(\frac{n-k+1}{k}\right) \cdot \frac{p}{q}$$

8 (d)

We have, $P(E_i) = \frac{1}{2}$ for $i = 1, 2, 3$

For $i \neq j$, we have,

$$P(E_i \cap E_j) = \frac{1}{4} = P(E_i)P(E_j)$$

$\Rightarrow E_i$ and E_j are independent events for $i \neq j$

$$\text{Also, } P(E_1 \cap E_2 \cap E_3) = \frac{1}{4} \neq P(E_1)P(E_2)P(E_3)$$

$\Rightarrow E_1, E_2, E_3$ are not independent

Hence option (d) is not correct

9 (a)

$$P(A) = 1 - P(\bar{A}) = 1 - \frac{2}{3} = \frac{1}{3}$$

Using, $P(A \cup B) = P(A) + P(B) - P(A \cap B)$

$$\Rightarrow \frac{3}{4} = \frac{1}{3} + P(B) - \frac{1}{4} \Rightarrow P(B) = \frac{2}{3}$$

$$\text{Now, } P(\bar{A} \cap B) = P(B) - P(A \cap B) = \frac{2}{3} - \frac{1}{4} = \frac{5}{12}$$

11 (a)

Let x, y and z be the parts and $x \leq y \leq z$. Then, $(x, y, z) \in (1, 1, 8), (1, 2, 7), (1, 3, 6), (1, 4, 5), (2, 2, 6), (2, 3, 5), (3, 3, 4), (2, 4, 4)$. Only the cases when (x, y, z) formed a triangle are $\{(3, 3, 4), (2, 4, 4)\}$,

$$\text{Required probability} = \frac{2}{8} = \frac{1}{4}$$

12 (b)

Let E_1 denote the event of travelling by train and E_2 denote the event travelling by plane.

$$P(E_1) = \frac{2}{3}, P(E_2) = \frac{1}{5}$$

$$P(E_1 \cup E_2) = P(E_1) + P(E_2)$$

$$= \frac{2}{3} + \frac{1}{5} = \frac{13}{15}$$

13 (a)

Three digit numbers multiple of 11 are 110, 121, ..., 990 (81 numbers). Now number also divisible by 9 are divisible by 99. So, numbers are 198, 297, ..., 990 (9 numbers).

So, required probability = $\frac{9}{81} = \frac{1}{9}$.

14 (b)

If any number the last digit can be 0, 1, 2, 3, 4, 5, 6, 7, 8, 9. We want that the last digit in the product is an odd digit other than 5 i.e. it is any one of the digits 1, 3, 7, 9. This means that the product is not divisible by 2 or 5. The probability that a number is divisible by 2 or 5 is $\frac{6}{10}$, and in the case the last digit can be one of 0, 2, 4, 5, 6 or 8. The probability that the number is not divisible by 2 or 5, is $1 - \frac{6}{10} = \frac{2}{5}$

In order that the product is not divisible by 2 or 5, none of the constituent numbers should be divisible by 2 or 5 and its probability is $\left(\frac{2}{5}\right)^4 = \frac{16}{125}$

15 (c)

Let E = Event of getting sum of 7 in two dice

$$= \{(1,6), (2,5), (3,4), (4,3), (5,2), (6,1)\}$$

Now, $P(E) = \frac{6}{36} = \frac{1}{6}$ (say)

$$\Rightarrow p = \frac{1}{6}$$

$$\therefore q = 1 - p = \frac{5}{6}$$

Required probability = ${}^4C_2 \left(\frac{1}{6}\right)^2 \left(\frac{5}{6}\right)^2$

$$= 6 \times \frac{5^2}{6^4} = \frac{25}{216}$$

16 (d)

The probability that Mr. A selected the loosing horse

$$= \frac{4}{5} \times \frac{3}{4} = \frac{3}{5}$$

The probability that Mr. A selected the winning horse

$$= 1 - \frac{3}{5} = \frac{2}{5}$$

17 (b)

Given, $S = \{1, 2, 3, \dots, 50\}$

$$A = \left\{n \in S : n + \frac{50}{n} > 27\right\}$$

$$= \{n \in S : n^2 - 27n + 50 > 0\}$$

$$= \{n \in S : n < 2 \text{ or } n > 25\}$$

$$= \{1, 26, 27, \dots, 50\}$$

$$\Rightarrow n(A) = 26$$

$$B = \{n \in S : n \text{ is a prime}\}$$

$$= \{2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47\}$$

$$\Rightarrow n(B) = 15$$

$$\therefore C = \{n \in S : n \text{ is a square}\}$$

$$= \{1, 4, 9, 16, 25, 36, 49\}$$

$$\Rightarrow n(C) = 7$$

$$\therefore P(A) = \frac{n(A)}{n(S)} = \frac{26}{50}, P(B) = \frac{15}{50}, P(C) = \frac{7}{50}$$

$$\Rightarrow P(A) > P(B) > P(C)$$

18 (c)

\therefore Required probability

$$= P(WBWB) + (BWBW)$$

$$= \frac{{}^5C_1 \times {}^3C_1 \times {}^4C_1 \times {}^2C_1}{{}^8C_1 \times {}^7C_1 \times {}^6C_1 \times {}^5C_1} + \frac{{}^3C_1 \times {}^5C_1 \times {}^2C_1 \times {}^4C_1}{{}^8C_1 \times {}^7C_1 \times {}^6C_1 \times {}^5C_1}$$

$$= 2 \left(\frac{5 \times 3 \times 4 \times 2}{8 \times 7 \times 6 \times 5} \right) = \frac{1}{7}$$

19 (c)

The total number of favourable cases, $n(E) = 18$

The total number of cases, $n(S) = {}^{20}C_3$

$$= \frac{20 \times 19 \times 18}{3 \times 2 \times 1} = 1140$$

$$\therefore \text{Required probability} = \frac{18}{1140} = \frac{3}{190}$$

20 (b)

The sum of two numbers is odd only when one is odd and other is even.

$$\therefore \text{Required probability} = \frac{{}^{20}C_1 \cdot {}^{20}C_1}{{}^{40}C_2}$$

$$= \frac{20 \times 20}{40 \times 39} = \frac{20 \times 20}{20 \times 39}$$

$$= \frac{2 \times 1}{2 \times 1}$$

$$= \frac{20}{39}$$

ANSWER-KEY

Q.	1	2	3	4	5	6	7	8	9	10
A.	C	A	A	C	B	B	A	D	A	B
Q.	11	12	13	14	15	16	17	18	19	20
A.	A	B	A	B	C	D	B	C	C	B

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