

Topic :-LINEAR INEQUALITIES

1. If a, b, c are positive real numbers such that $a + b + c = 2$ then, which one of the following is true?

- a) $(2 - a)(2 - b)(2 - c) \geq 8abc$
- b) $\frac{1}{a} + \frac{1}{b} + \frac{1}{c} \geq 2$
- c) $(2 - a)(2 - b)(2 - c) < 8abc$
- d) $\frac{1}{a} + \frac{1}{b} + \frac{1}{c} = 2$

2. If x, y, z are positive real numbers such that $x^2 + y^2 + z^2 = 27$, then $x^3 + y^3 + z^3$ has

- a) Minimum value 81
- b) Maximum value 81
- c) Minimum value 27
- d) Maximum value 27

3. If x satisfies the inequations $2x - 7 < 11$, $3x + 4 < -5$, then x lies in the interval

- a) $(-\infty, 3)$
- b) $(-\infty, 2)$
- c) $(-\infty, -3)$
- d) $(-\infty, \infty)$

4. $x^8 - x^5 - \frac{1}{x} + \frac{1}{x^4} > 0$, is satisfied for

- a) Only positive values of x
- b) Only negative values of x
- c) All real numbers except zero
- d) Only for $x > 1$

5. The solution set of the inequation $5^{(1/4)(\log_5 x)^2} \geq 5 x^{(1/5)(\log_5 x)}$, is

- a) $(0, 5^{-2\sqrt{5}}]$
- b) $[5^{2\sqrt{5}}, \infty)$
- c) $(0, 5^{-2\sqrt{5}}] \cup [5^{2\sqrt{5}}, \infty)$
- d) $(0, \infty)$

6. If $a + b = 8$, then ab is greater when

- a) $a = 4, b = 4$
- b) $a = 3, b = 5$
- c) $a = 6, b = 2$
- d) None of these

7. The number of solutions of the equation $\cos x + |x| = 0$ is

- a) 0
- b) 1
- c) 2
- d) 3

8. If $0 < x < \frac{\pi}{2}$, then the minimum value of $\frac{\cos^3 x}{\sin x} + \frac{\sin^3 x}{\cos x}$ is

- a) $\sqrt{3}$
- b) $\frac{1}{2}$
- c) $\frac{1}{3}$
- d) 1

9. If $x^2 + 4ax + 2 > 0$ for all values of x , then a lies in the interval
 a) $(-2, 4)$ b) $(1, 2)$ c) $(-\sqrt{2}, \sqrt{2})$ d) $(-\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}})$
10. If a and b are two different positive real numbers then which of the following statement is true?
 a) $2\sqrt{ab} > a + b$ b) $2\sqrt{ab} < a + b$ c) $2\sqrt{ab} = a + b$ d) None of these
11. The number of negative integral solutions of $x^2 \cdot 2^{x+1} + 2^{|x-3|+2} = x^2 \cdot 2^{|x-3|+4} + 2^{x-1}$, is
 a) None b) Only one c) Two d) Four
12. The number of ordered 4-tuples (x,y,z,w) where $x,y,z,w \in [0,10]$ which satisfy the inequality $2^{\sin^2 x} \times 3^{\cos^2 y} \times 4^{\sin^2 z} \times 5^{\cos^2 w} \geq 120$, is
 a) 81 b) 144 c) 0 d) Infinite
13. If $a > 1, b > 1, c > 1, d > 1$, then the minimum value of $\log_b a + \log_a b + \log_d c + \log_c d$ is
 a) 1 b) 2 c) 3 d) 4
14. The solution set of inequation $\log_{1/3}(2^{x+2} - 4^x) \geq -2$, is
 a) $(-\infty, 2 - \sqrt{13})$ b) $(-\infty, 2 + \sqrt{13})$ c) $(-\infty, 2)$ d) None of these
15. If $\frac{2x}{2x^2 + 5x + 2} > \frac{1}{x+1}$, then
 a) $-2 > x > -1$ b) $-2 \geq x \geq -1$ c) $-2 < x < -1$ d) $-2 < x \leq -1$
16. The number of real solutions of $\log_2 x + |x| = 0$, is
 a) 0 b) 1 c) 3 d) None of these
17. If $xyz = abc$, then the least value of $bcx + cay + abz$ is
 a) $3abc$ b) $6abc$ c) abc d) $4abc$
18. The number of solution(s) of the inequation $\sqrt{3x^2 + 6x + 7} + \sqrt{5x^2 + 10x + 14} \leq 4 - 2x - x^2$, is
 a) 1 b) 2 c) 4 d) Infinitely many
19. A stick of length 20 units is to be divided into n parts so that the product of the lengths of the parts is greater than unity. The maximum possible value of n is
 a) 18 b) 19 c) 20 d) 21
20. If a, b, c are different positive real number such that $(b + c - a), (c + a - b)$ and $(a + b - c)$ are positive, then $(a + b - c)(b + c - a)(c + a - b) - abc$ is
 a) Positive b) Negative c) Non-positive d) Non-negative