

**Topic :- CONIC SECTION**

- The value of  $m$ , for which the line  $y = mx + 2$  becomes a tangent to the conic  $4x^2 - 9y^2 = 36$  are  
a)  $\pm \frac{2}{3}$                       b)  $\pm \frac{2\sqrt{2}}{3}$                       c)  $\pm \frac{8}{9}$                       d)  $\pm \frac{4\sqrt{2}}{3}$
- If the tangent at the point  $P$  on the circle  $x^2 + y^2 + 6x + 6y = 2$  meets the straight line  $5x - 2y + 6 = 0$  at a point  $Q$  on the  $y$ -axis, then the length of  $PQ$  is  
a) 4                      b)  $2\sqrt{5}$                       c) 5                      d)  $3\sqrt{5}$
- Consider a family of circles, which are passing through the point  $(-1, 1)$  and are tangent to  $x$ -axis. If  $(h, k)$  are the coordinates of the centre of the circles, then the set of values of  $k$  is given by the interval  
a)  $0 < k < \frac{1}{2}$                       b)  $k \geq \frac{1}{2}$                       c)  $-\frac{1}{2} \leq k \leq \frac{1}{2}$                       d)  $k \leq \frac{1}{2}$
- The equation of the circle passing through the point  $(1, 1)$  and through the points of intersection of the circles  $x^2 + y^2 = 6$  and  $x^2 + y^2 - 6y + 8 = 0$  is  
a)  $x^2 + y^2 + 3y - 13 = 0$                       b)  $x^2 + y^2 - 3y + 1 = 0$   
c)  $x^2 + y^2 - 3x + 1 = 0$                       d)  $5x^2 + 5y^2 + 6y + 16 = 0$
- The number of distinct normal that can be drawn from  $(11/4, 1/4)$  to the parabola  $y^2 = 4x$ , is  
a) 3                      b) 2                      c) 1                      d) 4
- For the hyperbola  $\frac{x^2}{\cos^2 \alpha} - \frac{y^2}{\sin^2 \alpha} = 1$ , which of the following remains constant when  $\alpha$  varies?  
a) Eccentricity                      b) Directrix                      c) Abscissae of vertices                      d) Abscissae of foci
- The equation of the circumcircle of the triangle formed by the lines  $x = 0$ ,  $y = 0$ ,  $2x + 3y = 5$ , is  
a)  $6(x^2 + y^2) + 5(3x - 2y) = 0$   
b)  $x^2 + y^2 - 2x - 3y + 5 = 0$   
c)  $x^2 + y^2 + 2x - 3y - 5 = 0$   
d)  $6(x^2 + y^2) - 5(3x + 2y) = 0$

8. If  $t_1$  and  $t_2$  be the parameters of the end points of a focal chord for the parabola  $y^2 = 4ax$ , then which one is true?

- a)  $t_1 t_2 = 1$                       b)  $\frac{t_1}{t_2} = 1$                       c)  $t_1 t_2 = -1$                       d)  $t_1 + t_2 = -1$

9. The two circles

$$x^2 + y^2 - 2x + 22y + 5 = 0 \text{ and}$$

$x^2 + y^2 + 14x + 6y + k = 0$  intersect orthogonally provided  $k$  is equal to

- a) 47                      b) -47                      c) 49                      d) -49

10. The ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  and the straight line  $y = mx + c$  intersect in real points only if

- a)  $a^2 m^2 < c^2 - b^2$                       b)  $a^2 m^2 > c^2 - b^2$                       c)  $a^2 m^2 \geq c^2 - b^2$                       d)  $c \geq b$

11. If four points to be taken on a rectangular hyperbola such that the chord joining any two is perpendicular to the chord joining the other two and if  $\alpha, \beta, \gamma, \delta$  be the inclination to either asymptote of the straight line joining these points to the centre. Then,  $\tan \alpha \tan \beta \tan \gamma \tan \delta$  is equal to

- a) 1                      b) 0                      c) 2                      d) 3

12. If the distance between the foci and the distance between the directrices of the hyperbola  $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$  are in the ratio 3 : 2, then  $a : b$  is

- a)  $\sqrt{2} : 1$                       b)  $\sqrt{3} : \sqrt{2}$                       c) 1 : 2                      d) 2 : 1

13. If  $m_1$  and  $m_2$  are the slopes of tangents to the circle  $x^2 + y^2 = 4$  from the point (3, 2), then  $m_1 - m_2$  is equal to

- a)  $\frac{5}{12}$                       b)  $\frac{12}{5}$                       c)  $\frac{3}{2}$                       d) 0

14. The length of the axes of the conic  $9x^2 + 4y^2 - 6x + 4y + 1 = 0$ , are

- a)  $\frac{1}{2}, 9$                       b)  $3, \frac{2}{5}$                       c)  $1, \frac{2}{3}$                       d) 3, 2

15. For different values of  $\alpha$ , the locus of the point of intersection of the two straight lines  $\sqrt{3}x - y - 4\sqrt{3}\alpha = 0$  and  $\sqrt{3}\alpha x + ay - 4\sqrt{3} = 0$  is

- a) a hyperbola with eccentricity 2                      b) an ellipse with eccentricity  $\sqrt{\frac{2}{3}}$   
c) an hyperbola with eccentricity  $\sqrt{\frac{19}{16}}$                       d) an ellipse with eccentricity  $\frac{3}{4}$

16. If the area of the circle  $4x^2 + 4y^2 - 8x + 16y + k = 0$  is  $9\pi$  sq unit, then the value of  $k$  is

- a) 4                      b) 16                      c) -16                      d)  $\pm 16$

17.  $ABCD$  is a square whose side is  $a$ . The equation of the circle circumscribing the square, taking  $AB$  and  $AD$  as axes of reference, is

- a)  $x^2 + y^2 + ax + ay = 0$
- b)  $x^2 + y^2 + ax - ay = 0$
- c)  $x^2 + y^2 - ax - ay = 0$
- d)  $x^2 + y^2 - ax + ay = 0$

18. If the circle  $x^2 + y^2 + 2gx + 2fy + c = 0$  bisects the circumference of the circle  $x^2 + y^2 + 2g'x + 2f'y + c' = 0$ , then

- a)  $2g(g - g') + 2f(f - f') = c - c'$
- b)  $2g'(g - g') + 2f'(f - f') = c' - c$
- c)  $2g'(g - g') + 2f'(f - f') = c - c'$
- d)  $2g(g - g') + 2f(f - f') = c' - c$

19. If the parabolas  $y^2 = 4x$  and  $x^2 = 32y$  intersect at  $(16, 8)$  at an angle  $\theta$ , then  $\theta$  is equal to

- a)  $\tan^{-1}(3/5)$
- b)  $\tan^{-1}(4/5)$
- c)  $\pi$
- d)  $\pi/2$

20. The equation of the circle, which cuts orthogonally each of three circles

$$x^2 + y^2 - 2x + 3y - 7 = 0,$$

$$x^2 + y^2 + 5x - 5y + 9 = 0$$

and  $x^2 + y^2 + 7x - 9y + 29 = 0$

- a)  $x^2 + y^2 - 16x - 18y - 4 = 0$
- c)  $x^2 + y^2 - 16x = 0$

- b)  $x^2 + y^2 = a^2$
- d)  $y^2 - x^2 + 2x = 0$

