

## Topic :- CO-ORDINATE GEOMETRY

- If  $A$  and  $B$  are two points having coordinates  $(3, 4)$  and  $(5, -2)$  respectively and  $P$  is a point such that  $PA = PB$  and area of triangle  $PAB = 10$  sq unit, then the coordinates of  $P$  are  
a)  $(7, 4)$  and  $(13, 2)$     b)  $(7, 2)$  and  $(1, 0)$     c)  $(2, 7)$  and  $(4, 13)$     d) None of these
- In  $\Delta ABC$ ,  $\angle A = \frac{\pi}{2}$ ,  $b = 4$ ,  $c = 3$ , then the value of  $\frac{R}{r}$  is equal to  
a)  $\frac{5}{2}$     b)  $\frac{7}{2}$     c)  $\frac{9}{2}$     d)  $\frac{35}{24}$
- In the angles  $A$ ,  $B$  and  $C$  of a triangular are in the arithmetic progression and if  $a$ ,  $b$  and  $c$  denotes the lengths of the sides opposite to  $A$ ,  $B$  and  $C$  respectively, then the value of the expression  $\frac{a}{c}\sin 2C + \frac{c}{a}\sin 2A$  is  
a)  $\frac{1}{2}$     b)  $\frac{\sqrt{3}}{2}$     c) 1    d)  $\sqrt{3}$
- Two sides of a triangle are given by the roots of the equation  $x^2 - 5x + 6 = 0$  and the angle between the sides is  $\frac{\pi}{3}$ . Then, the perimeter of the triangle is  
a)  $5 + \sqrt{2}$     b)  $5 + \sqrt{3}$     c)  $5 + \sqrt{5}$     d)  $5 + \sqrt{7}$
- In a triangle  $ABC$ , if  $\angle A = 60^\circ$ ,  $a = 5$ ,  $b = 4$ , then  $c$  is a root of the equation  
a)  $c^2 - 5c - 9 = 0$     b)  $c^2 - 4c - 9 = 0$     c)  $c^2 - 10c + 25 = 0$     d)  $c^2 - 5c - 41 = 0$
- The angle of elevation of the top of vertical tower from a point  $A$  on the horizontal ground is found to be  $\frac{\pi}{4}$ . From  $A$ , a man walks 10 m up a path sloping at a angle  $\frac{\pi}{6}$ . After this the slope becomes steeper and after walking up another 10 m, the man reaches the top of the tower. Distance of  $A$  from the foot of the tower is  
a)  $5(1 + \sqrt{3})\text{m}$     b)  $\frac{5}{2}(1 + \sqrt{3})\text{m}$     c)  $5(\sqrt{3} - 1)\text{m}$     d)  $\frac{5}{2}(\sqrt{3} - 1)\text{m}$
- If the distance between the points  $(a\cos \theta, a\sin \theta)$  and  $(a\cos \phi, a\sin \phi)$  is  $2a$ , then  $\theta$  is equal to  
a)  $2n\pi \pm \pi + \phi, n \in Z$     b)  $n\pi + \frac{\pi}{2} + \phi, n \in Z$   
c)  $n\pi - \phi, n \in Z$     d)  $2n\pi + \phi, n \in Z$
- If  $A(0, 0)$ ,  $B(12, 0)$ ,  $C(12, 2)$ ,  $D(6, 7)$  and  $E(0, 5)$  are the vertices of the pentagon  $ABCDE$ , then its area in square units, is  
a) 58    b) 60    c) 61    d) 63

9. A flag is standing vertically on a tower of height  $b$ . On a point at a distance  $a$  from the foot of the tower, the flag and the tower subtend equal angles. The height of the flag is

- a)  $b \cdot \frac{a^2 + b^2}{a^2 - b^2}$       b)  $a \cdot \frac{a^2 - b^2}{a^2 + b^2}$       c)  $b \cdot \frac{a^2 - b^2}{a^2 + b^2}$       d)  $a \cdot \frac{a^2 + b^2}{a^2 - b^2}$

10. A kite is flying at an inclination of  $60^\circ$  with the horizontal. If the length of the thread is 120 m, then the height of the kite is

- a)  $60\sqrt{3}$  m      b) 60 m      c)  $\frac{60}{\sqrt{3}}$  m      d) 120 m

11.  $\frac{a \cos A + b \cos B + c \cos C}{a + b + c}$  is equal to

- a)  $1/r$       b)  $r/R$       c)  $R/r$       d)  $1/R$

12.  $AB$  is a vertical pole. The end  $A$  is on the level ground.  $C$  is the middle point of  $AB$ .  $P$  is a point on the level ground. The portion  $BC$  subtends an angle  $\beta$  at  $P$ . If  $AP = n AB$ , then  $\tan \beta =$

- a)  $\frac{n}{2n^2 + 1}$       b)  $\frac{n}{n^2 - 1}$       c)  $\frac{n}{n^2 + 1}$       d) None of these

13. If  $P(3,7)$  is a point on the line joining  $A(1,1)$  and  $B(6,16)$ , then the harmonic conjugate  $Q$  of point  $P$  has the coordinates

- a) (9, 29)      b) (-9, 29)      c) (9, -29)      d) (-9, -29)

14. The angles of a triangle are in the ratio 3:5:10. Then, the ratio of the smallest side to the greatest side is

- a)  $1:\sin 10^\circ$       b)  $1:2\sin 10^\circ$       c)  $1:\cos 10^\circ$       d)  $1:2\cos 10^\circ$

15. In  $\Delta ABC$ , if  $\begin{vmatrix} 1 & a & b \\ 1 & c & a \\ 1 & b & c \end{vmatrix} = 0$ , then

$\sin^2 A + \sin^2 B + \sin^2 C$  is equal to

- a)  $\frac{4}{9}$       b)  $\frac{9}{4}$       c)  $3\sqrt{3}$       d) 1

16. From a station  $A$  due West of a tower the angle of elevation of the top of the tower is seen to be  $45^\circ$ . From a station  $B$ , 10 m from  $A$  and in the direction  $45^\circ$  South of East of angle of elevation is  $30^\circ$ , the height of tower is

- a)  $5\sqrt{2}(\sqrt{5} + 1)$ m      b)  $\frac{5(\sqrt{5} + 1)}{2}$ m      c)  $\frac{5\sqrt{2}(\sqrt{5} + 1)}{2}$ m      d) None of these

17. A straight line with negative slope passing through the point (1, 4) meets the coordinate axes at  $A$  and  $B$ . The minimum value of  $OA + OB$  is equal to

- a) 5      b) 6      c) 9      d) 8

18. An observer finds that the elevation of the top of a tower is  $22\frac{1}{2}^\circ$  and after walking 150 metres towards the foot of the tower he finds that the elevation of the top has increased to  $67\frac{1}{2}^\circ$ . The height of the tower in metres is

- a) 50      b) 75      c) 125      d) 175

19. In an isosceles  $\Delta ABC$ ,  $AB = AC$ . If vertical angle  $A$  is  $20^\circ$ , then  $a^3 + b^3$  is equal to  
a)  $3a^2b$                       b)  $3b^2c$                       c)  $3c^2a$                       d)  $abc$

20. In a  $\Delta ABC$ ,  $a(\cos^2 B + \cos^2 C) + \cos A (c\cos C + b\cos B)$  is equal to  
a)  $a$                               b)  $b$                               c)  $c$                               d)  $a + b + c$

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