

Topic :- CO-ORDINATE GEOMETRY

- In ΔABC , $a^2(\cos^2 B - \cos^2 C) + b^2(\cos^2 C - \cos^2 A) + c^2(\cos^2 A - \cos^2 B)$ is equal to
a) 0 b) 1 c) $a^2 + b^2 + c^2$ d) $2(a^2 + b^2 + c^2)$
- If $\sin A : \sin B : \sin C = 3 : 4 : 5$, then $\cos A : \cos B$ is equal to
a) 4:3 b) 5:3 c) 3:4 d) 3:5
- If A, B, C are the angles of a triangle, then $\cot \frac{A}{2} + \cot \frac{B}{2} + \cot \frac{C}{2}$ is equal to
a) $\frac{s}{R}$ b) $\frac{R}{s}$ c) $\frac{\Delta}{s^2}$ d) $\frac{s^2}{\Delta}$
- Coordinates of the foot of the perpendicular drawn from $(0, 0)$ to the line joining $(a \cos \alpha, a \sin \alpha)$ and $(a \cos \beta, a \sin \beta)$ are
a) $(\frac{a}{2}, \frac{b}{2})$ b) $(\frac{a}{2}(\cos \alpha + \cos \beta), \frac{a}{2}(\sin \alpha + \sin \beta))$
c) $(\cos \frac{\alpha + \beta}{2}, \sin \frac{\alpha + \beta}{2})$ d) $(0, \frac{b}{2})$
- Three points are $A(6, 3), B(-3, 5), C(4, -2)$ and $P(x, y)$ is a point, then the ratio of area of ΔPBC and ΔABC is
a) $|\frac{x+y-2}{7}|$ b) $|\frac{x-y+2}{2}|$ c) $|\frac{x-y-2}{7}|$ d) None of these
- Two vertical poles 20 m and 80 m stands apart on a horizontal plane. The height of the point of intersection of the lines joining the top of each pole to the foot of the other is
a) 15 m b) 16 m c) 18 m d) 50 m
- A person on a ship sailing north sees two lighthouses which are 6 km apart, in a line due west. After an hour's sailing one of them bears south west and the other southern south west. The ship is travelling at a rate of
a) 12 km/hr b) 6 km/hr c) $3\sqrt{2}$ km/hr d) $(6 + 3\sqrt{2})$ km/hr
- If α, β, γ are the real roots of the equation $x^3 - 3px^2 + 3qx - 1 = 0$,
Then the centroid of the triangle whose vertices are $(\alpha, \frac{1}{\alpha}), (\beta, \frac{1}{\beta})$ and $(\gamma, \frac{1}{\gamma})$, is
a) (p, q) b) (q, p) c) $(-p, q)$ d) $(q, -p)$

9. If two vertices of a triangle are $(-2, 3)$ and $(5, -1)$. Orthocentre lies at the origin and centroid on the line $x + y = 7$, then the third vertex lies at
 a) $(7, 4)$ b) $(8, 14)$ c) $(12, 21)$ d) None of these
10. What is the equation of the locus of a point which moves such that 4 times its distance from the x -axis is the square of its distance from the origin?
 a) $x^2 + y^2 - 4y = 0$ b) $x^2 + y^2 - 4|y| = 0$ c) $x^2 + y^2 - 4x = 0$ d) $x^2 + y^2 - 4|x| = 0$
11. If $a^2 + b^2 = c^2$, then $s(s - a)(s - b)(s - c)$ is equal to
 a) a^2b^2 b) $\frac{1}{4}a^2b^2$ c) $\frac{1}{2}a^2b^2$ d) $\frac{1}{2}ab$
12. The harmonic conjugate of $(4, -2)$ with respect to $(2, -4)$ and $(7, 1)$ is
 a) $(-8, -14)$ b) $(2, 3)$ c) $(-2, -3)$ d) $(13, -5)$
13. If O is the origin and $P(x_1, y_1), Q(x_2, y_2)$ are two points, then $OP \cdot OQ \sin \angle POQ =$
 a) $x_1x_2 + y_1y_2$ b) $x_1y_2 + x_2y_1$ c) $|x_1y_2 - x_2y_1|$ d) None of these
14. If ΔABC , if $a = 3, b = 4, c = 5$, then the value of $\sin 2B$ is
 a) $4/5$ b) $3/20$ c) $24/25$ d) $1/50$
15. From an aeroplane vertically over a straight horizontal road, the angles of depression of two consecutive milestones on opposite sides of the aeroplane are observed to be α and β . The height of the aeroplane above the road is
 a) $\frac{\tan \alpha + \tan \beta}{\tan \alpha \tan \beta}$ b) $\frac{\tan \alpha \tan \beta}{\tan \alpha + \tan \beta}$ c) $\frac{\cot \alpha \cot \beta}{\cot \alpha + \cot \beta}$ d) None of these
16. In ΔABC , if $\angle A = 45^\circ, \angle B = 75^\circ$, then $a + c\sqrt{2}$ is equal to
 a) 0 b) 1 c) b d) $2b$
17. Three vertical poles of heights h_1, h_2 and h_3 at the vertices A, B and C of a ΔABC subtend angles α, β and γ respectively at the circumcentre of the triangle. If $\cot \alpha, \cot \beta$ and $\cot \gamma$ are in AP, then h_1, h_2, h_3 are in
 a) AP b) GP c) HP d) None of these
18. The area enclosed within the curve $|x| + |y| = 1$ is
 a) 1 sq unit b) $2\sqrt{2}$ sq units c) $\sqrt{2}$ sq units d) 2 sq units
19. P is a point on the segment joining the feet of two vertical poles of height a and b . The angles of elevation of the top of the poles from P are 45° each. Then, the square of the distance between the top of the poles is
 a) $\frac{a^2 + b^2}{2}$ b) $a^2 + b^2$ c) $2(a^2 + b^2)$ d) $4(a^2 + b^2)$
20. By rotating the coordinates axes through 30° in anticlockwise sense the equation $x^2 + 2\sqrt{3}xy - y^2 = 2a^2$ changes to
 a) $X^2 - Y^2 = 3a^2$ b) $X^2 - Y^2 = a^2$ c) $X^2 - Y^2 = 2a^2$ d) None of these