

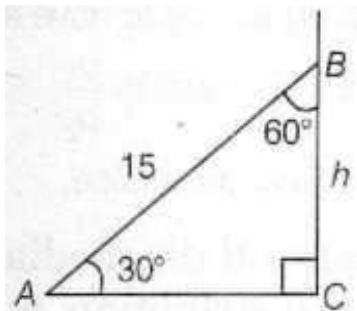
PAPER # 03 - MATHEMATICS

1. (d) The mid-point of line segment joining (0, 0) and (-4, -2) is $\left(\frac{0-4}{2}, \frac{0-2}{2}\right)$ i.e. (-2, -1).
2. (c) $\tan 45^\circ \cos 60^\circ + \sin 60^\circ \cot 60^\circ$
 $1 \times \frac{1}{2} + \frac{\sqrt{3}}{2} \times \frac{1}{\sqrt{3}} = \frac{1}{2} + \frac{1}{2} = 1$
3. (a) Given equation, $2x^2 - \sqrt{5}x + 1 = 0$
 On comparing it with $ax^2 + bx + c = 0$, we get
 $a = 2, b = \sqrt{5}$ and $c = 1$
 $\therefore D = (\sqrt{5})^2 - 4(2)(1)$ [$\because D = b^2 - 4ac$]
 $= 5 - 8 = -3$
4. (b) We have, $\sqrt{3} \sin \theta = \cos \theta$
 $\Rightarrow \frac{\sin \theta}{\cos \theta} = \frac{1}{\sqrt{3}} \Rightarrow \tan \theta = \frac{1}{\sqrt{3}}$
 $\Rightarrow \tan \theta = \tan 30^\circ \quad \theta = 30^\circ$
5. (d) Given, $AB \parallel EW$
 $\therefore \frac{DA}{AE} = \frac{DB}{BW}$ [by Thales theorem]
 $\Rightarrow \frac{DA}{DE - DA} = \frac{DB}{DW - DB}$
 $\Rightarrow \frac{4}{12 - 4} = \frac{DB}{24 - DB}$
 $\Rightarrow \frac{4}{8} = \frac{DB}{24 - DB}$
 $\Rightarrow 24 - DB = 2DB$
 $\Rightarrow 24 = 3DB$
 $\Rightarrow DB = \frac{24}{3} = 8 \text{ cm}$
6. (b) Let 4 be the event 'getting an even number.'
 Clearly, event A occurs, if we obtain any one of 2, 4, 6 as an outcome.
 \therefore Number of outcomes favourable to A = 3
 Hence, $P(A) = \frac{3}{6} = \frac{1}{2}$
7. (a) Length of the arc = $\frac{\theta}{360^\circ} \times 2\pi r$
 $\Rightarrow 4.4 = \frac{30^\circ}{360^\circ} \times 2 \times \frac{22}{7} \times r$
 $\Rightarrow 4.4 = \frac{1}{12} \times \frac{44}{7} \times r$
 $\Rightarrow r = \frac{4.4 \times 12 \times 7}{44} = 8.4 \text{ cm}$
8. (c) We know that
 Product of zeroes = $\frac{\text{Constant term}}{\text{Coefficient of } x^2}$
 $\therefore \alpha\beta = \frac{7}{4}$
9. (c) Total number of cards = 52
 Kings which are red in colour = 2
 $P(\text{king of red colour}) = \frac{2}{52} = \frac{1}{26}$
10. (a) If point P lies inside the circle then no tangent can be drawn.
11. (b) Let α and β be the zeros of the polynomial $f(x) = ax^2 + bx + c$. Then,
 $\alpha + \beta = -\frac{b}{a}$ and $\alpha\beta = \frac{c}{a}$
 Let S and P denote respectively the sum and product of the zeros of a polynomial whose zeros are $\frac{1}{\alpha}$ and $\frac{1}{\beta}$. Then,
 $S = \frac{1}{\alpha} + \frac{1}{\beta} = \frac{\alpha + \beta}{\alpha\beta} = \frac{-\frac{b}{a}}{\frac{c}{a}} = -\frac{b}{c}$ and
 $P = \frac{1}{\alpha} \times \frac{1}{\beta} = \frac{1}{\alpha\beta} = \frac{1}{\frac{c}{a}} = \frac{a}{c}$
 Hence, the required polynomial $g(x)$ is given by
 $g(x) = k(x^2 - Sx + P) = k\left(x^2 + \frac{bx}{c} + \frac{a}{c}\right)$,
 where k is any non-zero constant.

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12. (a) Class mark, frequency of the class

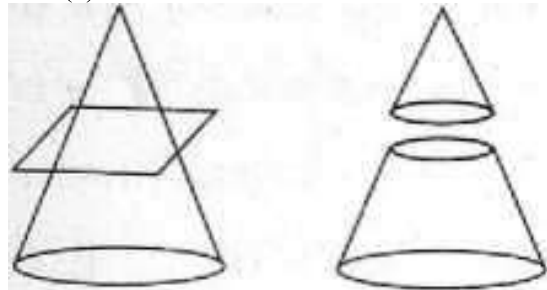
$$x = \frac{\sum fx}{\sum f} = \frac{\sum (A \times B)}{\sum A}$$
 where B is the class mark.
 Class mark = $\frac{1}{2}$ (upper limit + lower limit)
 and A is the frequency of the class.
13. (a) Let d be the common difference of the AR According to the question,
 $a_{17} - a_{10} = 7$
 $\Rightarrow (a + 16d) - (a + 9d) = 7 \Rightarrow 7d = 7 \Rightarrow d = 1$
14. (b) The mode is the most frequent observation. Here, the mode is 14 with a frequency of 15.
15. (d) $(x + 2)(3x - 5) = 0$
 $\Rightarrow x + 2 = 0$ or $3x - 5 = 0$
 $\Rightarrow x = -2$ or $x = \frac{5}{3}$
 Hence, the roots of the given equation are -2 and $\frac{5}{3}$.
16. (d) Given, equation $2x^2 - 6x + 7 = 0$
 On comparing it with $ax^2 + bx + c = 0$, we get
 $a = 2, b = -6$ and $c = 7$
 $\therefore D = b^2 - 4ac = (-6)^2 - 4(2)(7)$
 $= 36 - 56 = -20 < 0$
 So, the roots are imaginary.
17. (c) Given, $\angle ABC = 60^\circ$
 In $\triangle ABC$, $\angle BAC + \angle ABC + \angle ACB = 180^\circ$
 $\Rightarrow \angle BAC = 180^\circ - 90^\circ - 60^\circ = 30^\circ$



So, $\sin 30^\circ = \frac{BC}{AB} = \frac{h}{15}$

$$\Rightarrow \frac{1}{2} = \frac{h}{15} \Rightarrow h = \frac{15}{2} \text{ m}$$

18. (c) Circle



19. (c). Assertion Given $x + y - 8 = 0$ and $x - y - 2 = 0$
 Here, $a_1 = 1, b_1 = 1, c_1 = 8$
 and $a_2 = 1, b_2 = -1, c_2 = -2$
 So, $\frac{a_1}{a_2} = \frac{1}{1}, \frac{b_1}{b_2} = \frac{1}{-1}$ and $\frac{c_1}{c_2} = \frac{-8}{-2} = 4$
 $\therefore \frac{a_1}{a_2} \neq \frac{b_1}{b_2}$
 So, the system of equations has a unique solution and the Assertion is true.
Reason For equations to have a unique solution,
 $\frac{a_1}{a_2}$ should not be equal to $\frac{b_1}{b_2}$.
 \therefore The given Reason is false.
20. (a) Reason is clearly true.
 Using the relation given in reason, we have
 $2 \text{ Mean} = 3 \text{ Median} - \text{Mode}$
 $= 3 \times 150 - 154$
 $= 296$
 $\therefore \text{Mean} = \frac{296}{2} = 148$, which is true.
 Thus, both Assertion and Reason are true and Reason is the correct explanation of Assertion.
21. Given, $x = a \cos \theta$ and $y = b \sin \theta$
 $\therefore b^2 x^2 + a^2 y^2 = b^2 (a \cos \theta)^2 + a^2 (b \sin \theta)^2$ (1)
 $= a^2 b^2 \cos^2 \theta + a^2 b^2 \sin^2 \theta$
 $= a^2 b^2 (\cos^2 \theta + \sin^2 \theta)$
 $= a^2 b^2 (1) [\because \cos^2 A + \sin^2 A = 1]$
 $= a^2 b^2 (1)$

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22. Let us assume that $\frac{2}{5\sqrt{3}}$ is a rational number.

$\therefore \frac{2}{5\sqrt{3}} = \frac{p}{q}$, where p,q (q \neq 0) are integers and p, q are coprimes. (1)

$$\Rightarrow \frac{2q}{5p} = \sqrt{3}$$

Since, 2, 5, p and q are integers.

$\therefore \frac{2q}{5p}$ is rational, so $\sqrt{3}$ is rational.

But this contradicts the fact that $\sqrt{3}$ is irrational.

Hence, $\frac{2}{5\sqrt{3}}$ is an irrational number.

Hence proved. (1)
OR

Let us assume that $6 - 2\sqrt{3}$ is rational number.

Then, it will be of the form $\frac{a}{b}$, where a, b are coprime integers and b \neq 0.

$$\text{Now, } 6 - 2\sqrt{3} = \frac{a}{b}$$

On rearranging, we get

$$6 - \frac{a}{b} = 2\sqrt{3} \quad (1)$$

Since, 6 and $\frac{a}{b}$ are rational. So, their difference will be rational.

$\therefore 2\sqrt{3}$ is rational.

But we know that, $\sqrt{3}$ is irrational.

So, this contradicts the fact that $\sqrt{3}$ is irrational.

Therefore, our assumption is wrong.

Hence, $6 - 2\sqrt{3}$ is irrational.

Hence proved. (1)

23. We have, $p(x) = 5x^2 - 7x + 1$, whose zeroes are α and β .

$$\therefore \text{Sum of zeroes, } \alpha + \beta = -\frac{\text{Coefficient of } x}{\text{Coefficient of } x^2}$$

$$= -\frac{(-7)}{5} = \frac{7}{5} \dots(i) \quad (1)$$

and product of zeroes, $\alpha\beta = \frac{\text{Constant term}}{\text{Coefficient of } x^2}$

$$= \frac{1}{5} \dots(ii)$$

$$\text{Now, } \frac{1}{\alpha} + \frac{1}{\beta} = \frac{\beta + \alpha}{\alpha\beta} = \frac{7/5}{1/5}$$

[from Eqs. (i) and (ii)]

$$= 7 \quad (1)$$

24. We have, $\frac{1}{x+1} + \frac{2}{x+2} = \frac{4}{x+4}$

$$\Rightarrow \frac{(x+2) + 2(x+1)}{(x+1)(x+2)} = \frac{4}{x+4} \quad (1)$$

$$\Rightarrow (x+4)(3x+4) = 4(x^2 + 3x + 2)$$

$$\Rightarrow x^2 - 4x - 8 = 0$$

On comparing it with $ax^2 + bx + c = 0$, we get

$$a = 1, b = -4 \text{ and } c = -8$$

$$\therefore x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\Rightarrow x = \frac{-(-4) \pm \sqrt{16 - 4(1)(-8)}}{2} = x = \frac{4 \pm \sqrt{48}}{2}$$

$$\Rightarrow x = 2 \pm 2\sqrt{3} \quad (1)$$

25. $\therefore \Delta AGF \sim \Delta DBG \dots(i)$

[by AA similarity criterion]

Now, in ΔAGF and ΔEFC , we get

$$\angle FAG = \angle CEF \text{ [each } 90^\circ]$$

and $\angle AFG = \angle ECF$ [corresponding angles because $GF \parallel BC$ and AC is the transversal]

$$\therefore \Delta AGF \sim \Delta EFC \dots(ii) \quad (1)$$

From Eqs. (i) and (ii), we get

$$\Delta DBG \sim \Delta EFC$$

$$\Rightarrow \frac{BD}{EF} = \frac{DG}{EC}$$

$$\Rightarrow \frac{BD}{DE} = \frac{DE}{EC} \text{ [}\because \text{ DEFG is a square]}$$

$$\therefore DE^2 = BD \times EC \text{ Hence proved. (1)}$$

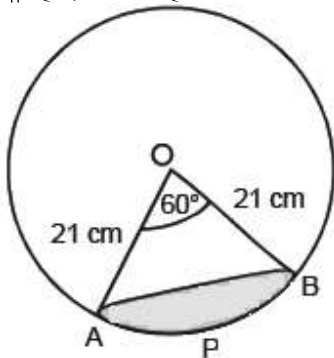
OR

Given,

In ΔPQO , $DE \parallel OQ$

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So by using Basic Proportionality Theorem,
 $PD/DO = PE/EQ$ (i)
 Again given, in ΔPOR , $DF \parallel OR$,
 So by using Basic Proportionality Theorem,
 $PD/DO = PF/FR$ (ii)
 From equation (i) and (ii), we get,
 $PE/EQ = PF/FR$
 Therefore, by converse of Basic Proportionality Theorem,
 $EF \parallel QR$, in ΔPQR .



26.

Given,
 Radius = 21 cm
 $\theta = 60^\circ$

(i) Length of an arc = $\theta/360^\circ \times \text{Circumference}$ ($2\pi r$)

$$\begin{aligned} \therefore \text{Length of an arc AB} &= (60^\circ/360^\circ) \times 2 \times (22/7) \times 21 \\ &= (1/6) \times 2 \times (22/7) \times 21 \end{aligned}$$

Or Arc AB Length = 22cm

(ii) It is given that the angle subtended by the arc = 60°

So, the area of the sector making an angle of 60°

$$\begin{aligned} &= (60^\circ/360^\circ) \times \pi r^2 \text{ cm}^2 \\ &= 441/6 \times 22/7 \text{ cm}^2 \end{aligned}$$

Or, the area of the sector formed by the arc APB is 231 cm^2

(iii) Area of segment APB = Area of sector OAPB – Area of ΔOAB

Since the two arms of the triangle are the radii of the circle and thus are equal, and one angle is 60° , ΔOAB is an equilateral triangle. So, its area will be $\sqrt{3}/4 \times a^2$ sq. Units.

The area of segment APB = $231 - (\sqrt{3}/4) \times (OA)^2$

$$= 231 - (\sqrt{3}/4) \times 21^2$$

Or, the area of segment

$$APB = [231 - (441 \times \sqrt{3})/4] \text{ cm}^2$$

27. Given A circle inscribed in a ΔPQR such that

$PQ = PR$

To prove $QT = TR$

Proof We know that the tangents from an external points to a circle are equal in length.

$PS = PU$ [tangents from P] ... (i)

$QS = QT$ [tangents from O] ... (ii)

$RT = RU$ [tangents from R] ... (iii)

Now, $PQ = PR$ [given] ($1 \frac{1}{2}$)

$$\Rightarrow PQ - PS = PR - PS$$

[subtracting PS from both sides]

$$\Rightarrow PQ - PS = PR - PU \text{ [from Eq. (i)]}$$

$$\Rightarrow QS = RU$$

$$\Rightarrow QT = RU \text{ [from Eq. (ii)]}$$

$$\Rightarrow QT = RT \text{ [from Eq. (iii)]}$$

Hence proved. ($1 \frac{1}{2}$)

28. There are 6 possible outcomes (1, 2, 3, 4, 5 and 6) in a single throw of a die.

(i) We know that even prime number is only 2.

So, number of favourable outcomes = 1

$$\therefore P(\text{getting an even prime number}) = \frac{1}{6} \text{ (1 } \frac{1}{2}\text{)}$$

(ii) The numbers divisible by 2 are 2, 4 and 6.

So, number of favourable outcomes = 3

$\therefore P(\text{getting a number divisible by 2})$

$$= \frac{3}{6} = \frac{1}{2}$$

OR

Number of red cards = 26

Number of queens = 4

But, out of these 4 queens, 2 are red.

\therefore Number of queens which are not red = 2

Now, number of cards which are red or queen

$$= 26 + 2 = 28 \text{ (1)}$$

$\therefore P(\text{getting either red card or queen})$

$$= \frac{\text{Number of card which are red or queen}}{\text{Total number of cards}}$$

Total number of cards

$$= \frac{28}{52} = \frac{7}{13} \text{ (1)}$$

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Now, P (not getting either red card or queen)

= 1 - P (getting either red card or queen)

$$= 1 - \frac{7}{13} = \frac{13-7}{13} = \frac{6}{13}$$

29. Here, class intervals are not in inclusive form.

So, we first convert them in inclusive form by subtracting $h/2$ from the lower limit and adding $h/2$ to the upper limit of each class, where h is the difference between the lower limit of a class and the upper limit of the preceding class.

The given frequency distribution in inclusive form is as follows.

Age (in yr)	Number of cases
4.5-14.5	6
14.5-24.5	11
24.5-34.5	21
34.5-44.5	23
44.5-54.5	14
54.5-64.5	5

(1)

We observe that the class 34.5-44.5 has the maximum frequency.

So, it is the modal class such that

$I = 34.5$, $h = 10$, $f_1 = 23$, $f_0 = 21$ and $f_2 = 14$

$$\therefore \text{Mode} = I + \frac{f_1 - f_0}{2f_1 - f_0 - f_2} \times h,$$

$$\Rightarrow \text{Mode} = 34.5 + \frac{23-21}{46-21-14} \times 10$$

$$= 34.5 + \frac{2}{11} \times 10 = 36.31 \quad (1)$$

30. The given equations are

$$10x + 3y = 75 \dots(i)$$

$$6x - 5y = 11 \dots (ii)$$

Multiplying Eq. (i) by 5 and Eq. (ii) by 3, we get

$$50x + 15y = 375 \dots(iii)$$

$$18x - 15y = 33 \dots(iv) (1)$$

Adding Eqs. (iii) and (iv), we get

$$68x = 408$$

$$\Rightarrow x = \frac{408}{68} \Rightarrow x = 6 (1)$$

Putting $x = 6$ in Eq.(i), we get

$$(10 \times 6) + 3y = 75$$

$$\Rightarrow 60 + 3y = 75$$

$$\Rightarrow 3y = 75 - 60$$

$$\Rightarrow 3y = 15$$

$$\Rightarrow y = 5$$

$$\therefore x = 6 \text{ and } y = 5 (1)$$

OR

The given equations are

$$11x + 15y + 23 = 0 \dots (i)$$

$$7x - 2y - 20 = 0 \dots(ii)$$

Multiplying Eq. (i) by 2 and Eq. (ii) by 15 and adding the results, we get

$$22x + 105x = -46 + 300$$

$$\Rightarrow 127x = 254$$

$$\Rightarrow x = \frac{254}{127} = 2 (1)$$

Putting $x = 2$ in Eq. (i), we get

$$22 + 15y = -23$$

$$\Rightarrow 15y = -23 - 22$$

$$\Rightarrow 15y = -45$$

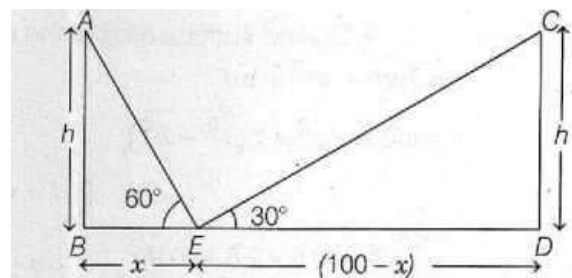
$$\Rightarrow y = \frac{-45}{15} \Rightarrow y = -3$$

Hence, $x = 2$ and $y = -3 (2)$

31. Let AB and CD be two pillars of equal height h and distance between them be $BD = 100$ m.

Let E be a point on the road such that $BE = x$,

$DE = (100 - x)$, $\angle AEB = 60^\circ$ and $\angle CED = 30^\circ$.



In right angled $\triangle ABE$,

$$\frac{AB}{BE} = \tan 60^\circ$$

$$\Rightarrow \frac{h}{x} = \sqrt{3} \quad [\because \tan 60^\circ = \sqrt{3}]$$

$$\Rightarrow h = \sqrt{3} x \dots (i) (1)$$

In right angled $\triangle CDE$,

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$$\frac{CD}{DE} = \tan 30^\circ$$

$$\Rightarrow \frac{h}{100-x} = \frac{1}{\sqrt{3}} \dots(ii) (1)$$

From Eqs. (i) and (ii); we get

$$\sqrt{3} = \frac{100-x}{\sqrt{3}}$$

$$\Rightarrow 3x = 100 - x \quad \Rightarrow 4x = 100$$

$$\therefore x = 25$$

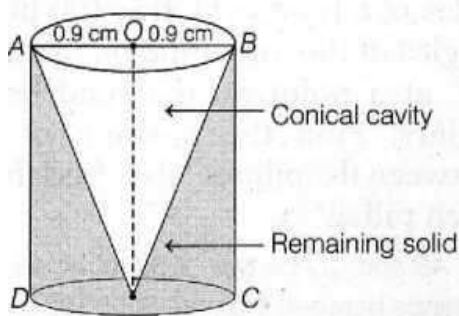
On putting $x = 25$ in Eq. (i), we get

$$h = \sqrt{3} \times 25$$

$$= 25 \times 1.732 = 43.3 \text{ m}$$

Hence, height of each pillar is 43.3 m and position of the point from pillar making an angle of 60° is 25 m. (1)

32. Let's be the total surface area of the remaining solid.



Then, S = Curved surface area of the cylinder + Area of the base of the cylinder + Curved surface area of the cone

$$= 2\pi rh + \pi r^2 + \pi r l \quad (1)$$

$$= \pi [2rh + r^2 + r\sqrt{r^2 + h^2}]$$

$$[\because l = \sqrt{r^2 + h^2}]$$

$$= \frac{22}{7} [5.04 + 0.81 + 0.9\sqrt{0.81 + 7.84}]$$

$$= \frac{22}{7} [5.85 + 0.9\sqrt{8.65}]$$

$$= \frac{22}{7} [5.85 + 0.9 \times 2.94]$$

$$= \frac{22}{7} \times [5.85 + 2.64] = \frac{186.78}{7}$$

$$= 26.68 \text{ cm}^2 \quad (2)$$

OR

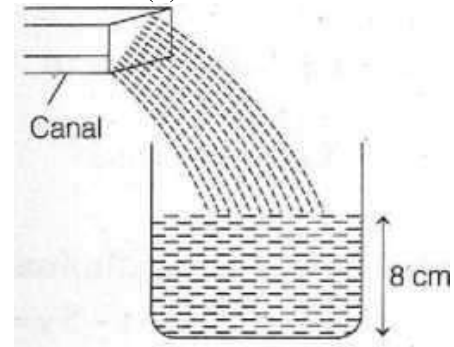
Given, speed of flow of water = 10 km /h
 $= 10 \times 1000 \text{ m/h} [\because 1 \text{ km} = 1000 \text{ m}]$

\Rightarrow Length of water flow in 1 h = $10 \times 1000 \text{ m}$

\Rightarrow Length of water flow in 30 min (i.e. in $\frac{1}{2}$ h)

$$= \frac{1}{2} \times 10 \times 1000$$

$$= 5000 \text{ m} (1)$$



(1)

Now, volume of water flowing in 30 min
 $=$ Volume of cuboid of length 5000 m, width 6 m and depth 1.5 m

$$= 5000 \times 6 \times 1.5 \text{ m}^3 = 45000 \text{ m}^3 (1)$$

Hence, the required area covered for irrigation with 8 cm or m of standing water

$$= \frac{4500}{8} \times 100 = 562500 \text{ m}^2$$

$$= \frac{562500}{1000} \text{ hec} [\because 1 \text{ hec} = 10000 \text{ m}^2]$$

$$= 56.25 \text{ hec} (2)$$

33. Given, equations are $5x - y = 5 \dots(i)$

and $3x - y = 3 \dots(ii)$

Table for $5x - y = 5$ or $y = 5x - 5$ is

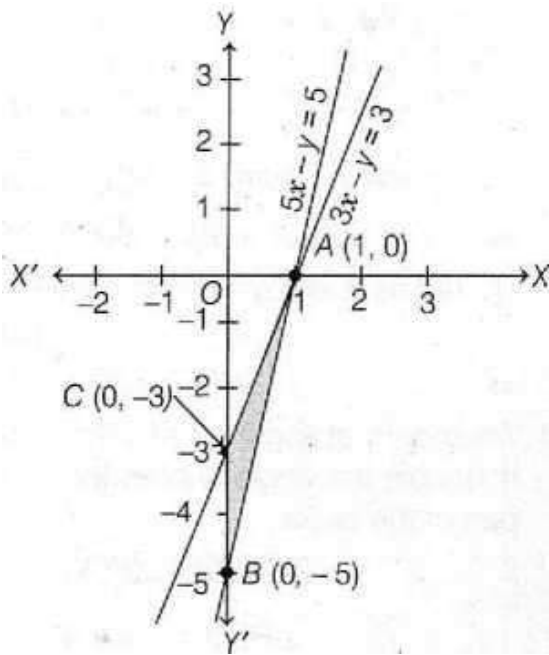
X	1	0
Y	0	-5
Points	A (1,0)	B (0, -5)

Plot the points A(1, 0) and B(0, -5) on a graph paper and join these points to form line AB. (1)

Table for $3x - y = 3$ or $y = 3x - 3$ is

X	1	0
Y	0	-3
Points	A (1, 0)	C (0, -3)

Plot the points A (1, 0) and C (0, -3) on the same graph paper and join these points to form line AC. (1)

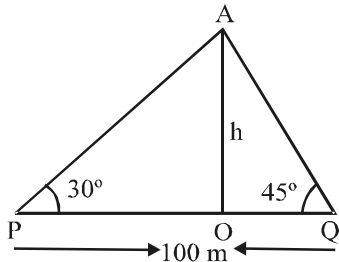


(2)

Hence, the triangle formed by given lines is $\triangle ABC$ whose vertices are $A(1, 0)$, $B(0, -5)$ and $C(0, -3)$.

(1)

34. Let OA be the tree of height h metre. In triangles POA and QOA , we have
 $\tan 30^\circ = \frac{OA}{OP}$ and $\tan 45^\circ = \frac{OA}{OQ}$



$$\begin{aligned} \Rightarrow \frac{1}{\sqrt{3}} &= \frac{h}{OP} \text{ and } 1 = \frac{h}{OQ} \\ \Rightarrow OP &= \sqrt{3}h \text{ and } OQ = h \\ \Rightarrow OP + OQ &= \sqrt{3}h + h \\ \Rightarrow PQ &= (\sqrt{3} + 1)h \\ \Rightarrow 100 &= (\sqrt{3} + 1)h \text{ [}\because PQ = 100 \text{ m]} \\ \Rightarrow h &= \frac{100}{\sqrt{3} + 1} \text{ m} \\ \Rightarrow h &= \frac{100(\sqrt{3} - 1)}{2} \text{ m} \\ \Rightarrow h &= 50(1.732 - 1) \text{ m} = 36.6 \text{ m} \end{aligned}$$

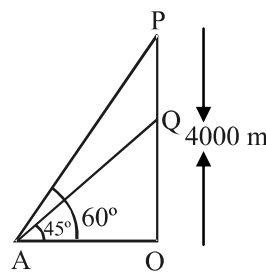
Hence, the height of the tree is 36.6 m

OR

Let P and Q be the positions of two aeroplanes when Q is vertically below P and $OP = 4000$ m. Let the angles of elevation of P and Q at a point A on the ground be 60° and 45° respectively.

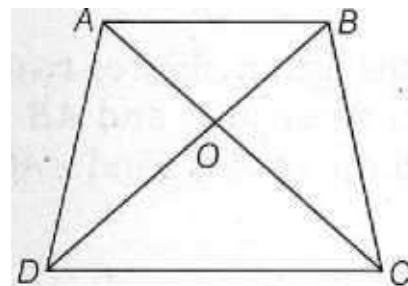
In triangles AOP and AOQ , we have

$$\begin{aligned} \tan 60^\circ &= \frac{OP}{OA} \text{ and } \tan 45^\circ = \frac{OQ}{OA} \\ \Rightarrow \sqrt{3} &= \frac{4000}{OA} \text{ and } 1 = \frac{OQ}{OA} \\ \Rightarrow OA &= \frac{4000}{\sqrt{3}} \text{ and } OQ = OA \\ \Rightarrow OQ &= \frac{4000}{\sqrt{3}} \text{ m} \end{aligned}$$



$$\begin{aligned} \therefore \text{Vertical distance between the aeroplanes} \\ &= PQ = OP - OQ \\ &= \left(4000 - \frac{4000}{\sqrt{3}}\right) \text{ m} = 4000 \frac{(\sqrt{3} - 1)}{\sqrt{3}} \text{ m} \\ &= 1690.53 \text{ m} \end{aligned}$$

35. Given $ABCD$ is a trapezium in which $AB \parallel DC$.



To prove $\frac{OA}{OC} = \frac{OB}{OD}$ (2)

Proof In $\triangle OAS$ and $\triangle ODC$, we have
 $AB \parallel DC$

Then, $\angle OAB = \angle OCD$ [alternate interior angles]

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$\angle AOB = \angle DOC$ [vertically opposite angles]

and $\angle ABO = \angle CDO$ [alternate interior angles]

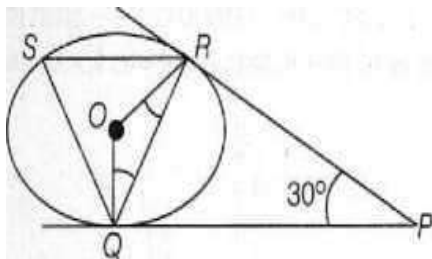
$\therefore \Delta OAB \sim \Delta OCD$ [by AAA similarity criterion]

Hence, $\frac{OA}{OC} = \frac{OB}{OD}$

[if two triangles are similar, then their corresponding sides are proportional]

Hence proved. (1)

36. (i) In quadrilateral POOR, we have



$$\begin{aligned} \angle QPR + \angle PRO + \angle PQO + \angle ROQ &= 360^\circ \\ \Rightarrow 30^\circ + 90^\circ + 90^\circ + \angle ROQ &= 360^\circ \end{aligned}$$

[\because radius is always perpendicular to the tangent at point of contact]

$$\Rightarrow \angle ROQ = 360^\circ - 210^\circ = 150^\circ$$

- (ii) We know that angle subtended by an arc at centre is double the angle subtended by it at any other part of the circle.

$$2 \angle RSQ = \angle ROQ$$

$$\angle RSQ = \frac{1}{2} \times 150^\circ = 75^\circ$$

- (iii) In ΔQOR , $OQ = OR$ [radii]

$$\angle ORQ = \angle OQR$$

$$\text{Now, } \angle ROQ + \angle ORQ + \angle OQR = 180^\circ$$

$$\Rightarrow 2\angle OQR = 180^\circ - 150^\circ$$

$$\Rightarrow 2\angle OQR = 30^\circ$$

$$\Rightarrow \angle OQR = 15^\circ$$

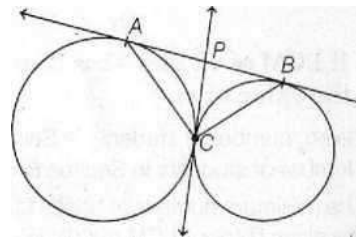
Again, $\angle OQP = 90^\circ$ [$\because OQ \perp QP$]

$$\Rightarrow \angle OQR + \angle RQP = 90^\circ$$

$$\Rightarrow \angle RQP = 90^\circ - 15^\circ = 75^\circ$$

OR

Draw a tangent to the circles at point C. Let it meet AB at P



Then, $PA = PC$ and $PS = PC$

[the tangents from an external points to a circle are equal in length]

$$PA = PC \Rightarrow \angle PAC = \angle PCA$$

$$PB = PC \Rightarrow \angle PBC = \angle PCB$$

$$\therefore \angle PAC + \angle PBC = \angle PCA + \angle PCB = \angle ACB$$

$$\Rightarrow \angle PAC + \angle PBC + \angle ACB = 2\angle ACB$$

$$\Rightarrow 180^\circ = 2\angle ACB$$

$$\Rightarrow \angle ACB = 90^\circ$$

37. (i) For first metre, the charge is Rs. 100

i.e. first term, $a = 100$

As, there is increasing of Rs. 25 for each subsequent metres, therefore common difference, $d = 25$

So, the AP thus formed is

$$100, 125, 150, \dots$$

- (ii) Labour charge to dig the well is the 15th term of AP.

We know, $a_n = a + (n - 1)d$

$$\therefore a_{15} = 100 + (15 - 1)25$$

$$= 100 + 14 \times 25 = 450$$

$$\therefore \text{Labour charge} = \text{Rs. } 450$$

- (iii) Money saved by Ram = Rs. 450 - Rs. 400 = Rs. 50

OR

We know that $S_n = \frac{n}{2} [2a + (n - 1)d]$

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$$\text{Sum of 15 terms, } S_{15} = \frac{15}{2} [2 \times 100 + 14 \times 25]$$

$$= \frac{15}{2} [200 + 350] = \frac{15}{2} \times 550 = 4125$$

38. (i) Given, number of students in Section A = 32

Number of students in Section B = 36

The minimum number of books to be acquired for the class library = LCM of (32, 36)

$$= 2 \times 2 \times 2 \times 2 \times 2 \times 3 \times 3$$

$$= 2^5 \times 3^2$$

$$= 32 \times 9 = 288$$

- (ii) The prime factors of 36 are

$$36 = 2 \times 2 \times 3 \times 3 = 2^2 \times 3^2$$

- (iii) HCF (867, 255) = 51

OR

Given, LCM (12, 42) = 10m + 4

Factors of 12 = 2 × 2 × 3

and factors of 42 = 2 × 3 × 7

Now, LCM (12, 42) = 2 × 2 × 3 × 7 = 84

$$\therefore 84 = 10m + 4$$

$$\Rightarrow 84 - 4 = 10m$$

$$\therefore m = \frac{80}{10} = 8$$